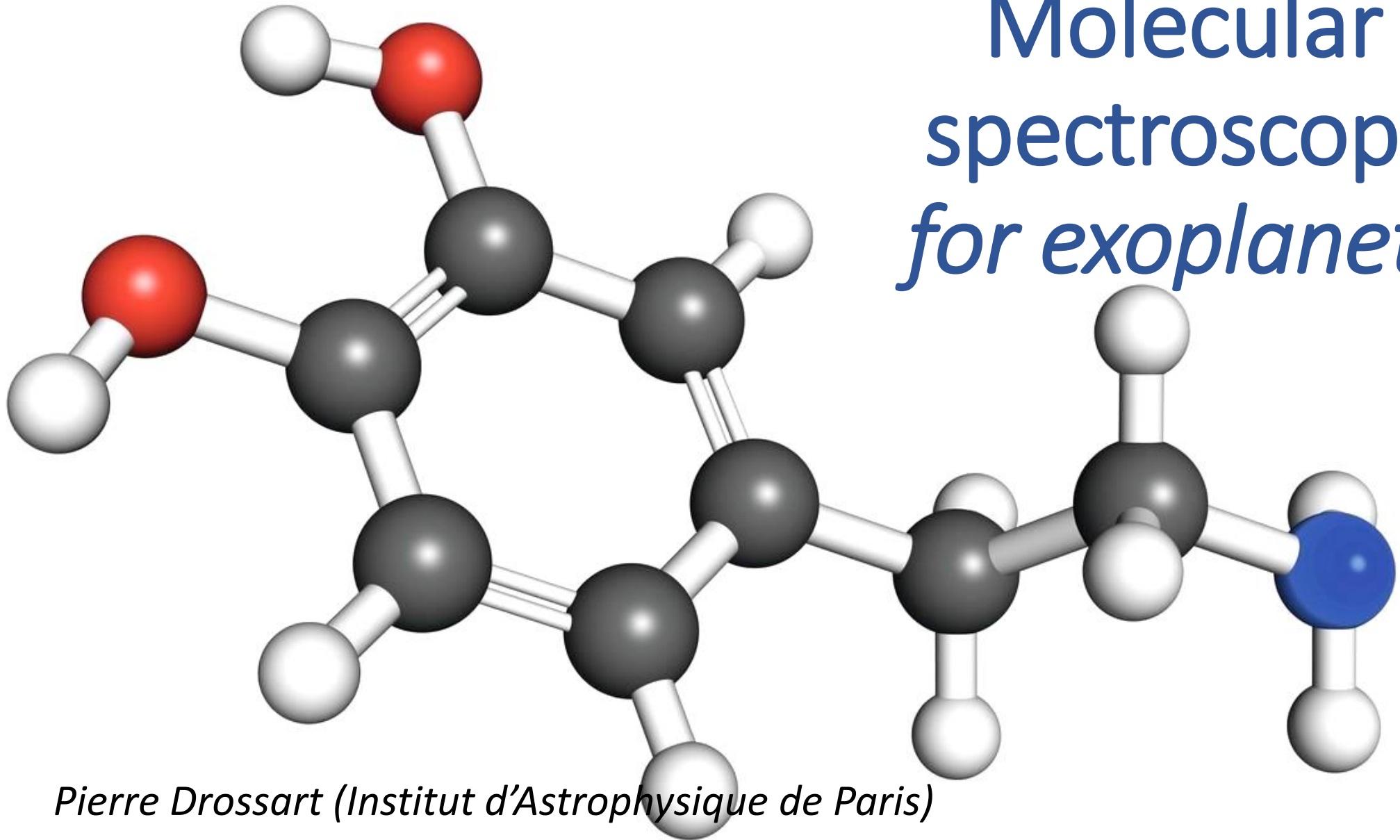


Molecular spectroscopy *for exoplanets*



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& Isabelle Kleiner (LISA, Univ. Créteil)*

Credits

- Isabelle Kleiner, Les Houches course (Ariel school 2022)
- Herzberg : Infrared and Raman spectra of polyatomic molecules
- Spectral line shapes course : Professor Ronald K. Hanson
<https://cefrc.princeton.edu/sites/g/files/toruqf1071/files/documents/Lecture%20Notes%20-%20Hanson.pdf>
- Exomol : Tennyson et al, JQSRT 2020 (The 2020 release of the ExoMol database: Molecular line lists for exoplanet and other hot atmospheres)
- The spectroscopic community : I. Kleiner, M. Rey, V. Boudon, J. Tennyson, V. Tyuterev,... – (*Paris, Reims, Dijon, Rennes, London, Omsk*)

Topics in Molecular spectroscopy

1. **Concepts : spectroscopy and the rotation and vibration of molecules**
2. **Diatomic molecules**
 - a. The rigid rotator in quantum mechanics
 - b. The harmonic oscillator in quantum mechanics
3. **Polyatomic molecules :**
 - a. Linear molecules : CO₂
 - b. Spherical tops : CH₄
 - c. Symmetric tops : NH₃
 - d. Asymmetric tops : H₂O
4. **Thermodynamics**
 - a. Population of vibro-rotational levels
 - b. Partition functions
5. **Line widths and absorption coefficients**
 - a. Lorentz shape
 - b. Doppler shape
 - c. Voigt shape
6. **Some special effects**
 - a. Far wings
 - b. Collision induced absorption
7. **Data bases**

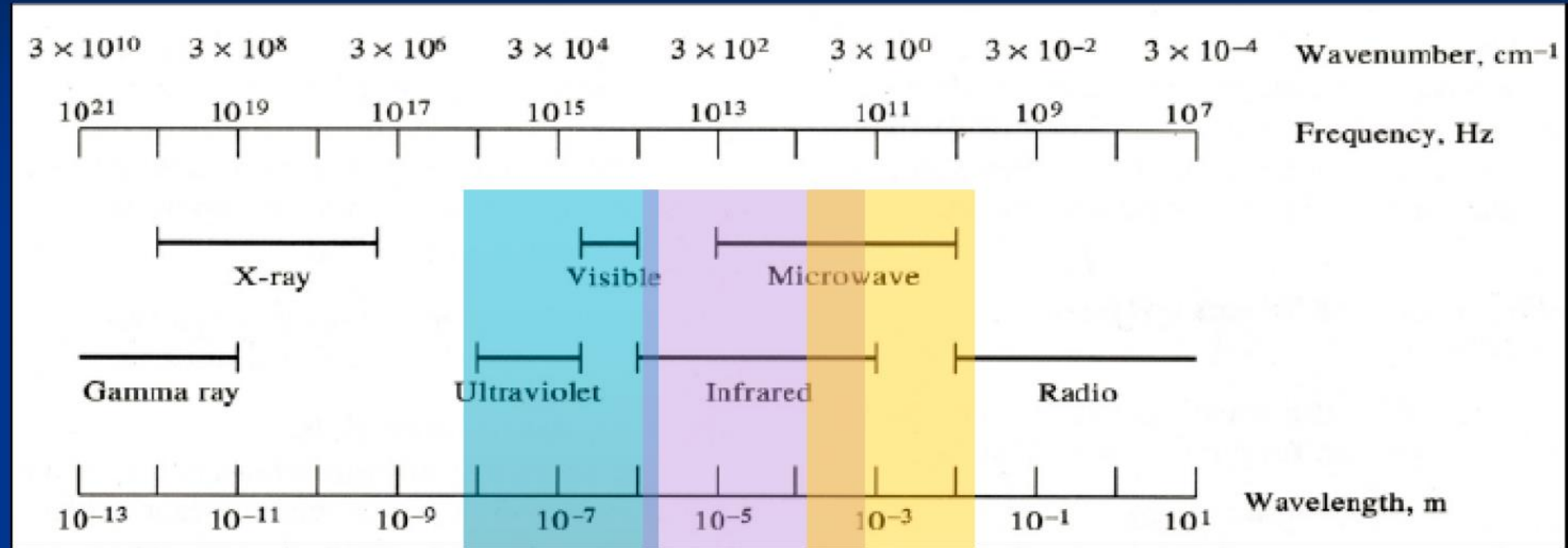
Matter – radiation models for exoplanets

A large part of astrophysics models rely on matter – radiation interaction. In planetary atmospheres, one encounters various phenomena:

- Scattering phenomena (molecular => Rayleigh or particulate => Mie or similar model)
- Molecule-photon interaction in thermal emission or stellar radiation transfer

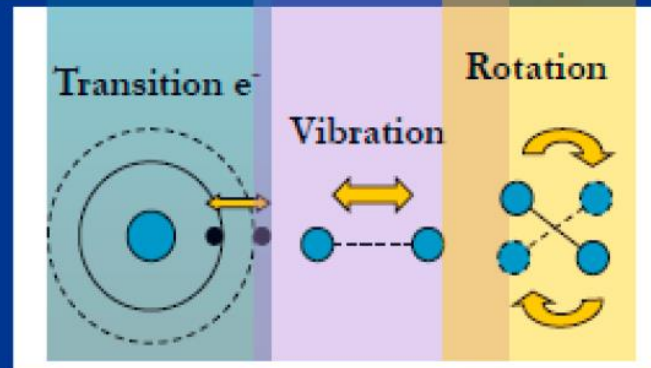
Here, we explore the molecular models : quantum mechanics is at the base of the description of molecule states. For radiation/molecule model, radiative transfer approximation will treat the light in a classical matter – full quantum radiation/molecule models are usually not necessary => Quantum mechanics is usually limited to the matter domain.

Spectral range and molecular motions



Interaction

Rayonnement-Matière



The Born-Oppenheimer approximation

Due to the large difference in the masses of the nuclei and of the electron, the Born-Oppenheimer approximation stipules that the electronic part of the wave function can be decoupled from the nucleus part with q_i the electronic and Q_i the nuclear coordinates

$$\Psi(q_i, Q_i) = \Psi_{el}(q_i; Q_i) \Psi_N(Q_i)$$

The total energy of the molecule is the sum of

- An electronic part
- A vibrational part
- A rotational part

Which are solved independently

Electronic structure is solved by “freezing” the nuclei at fixed positions and by resolving electronic Schrödinger equation :

$$H_{el} \Psi_{el} = E_{el} \Psi_{el}$$

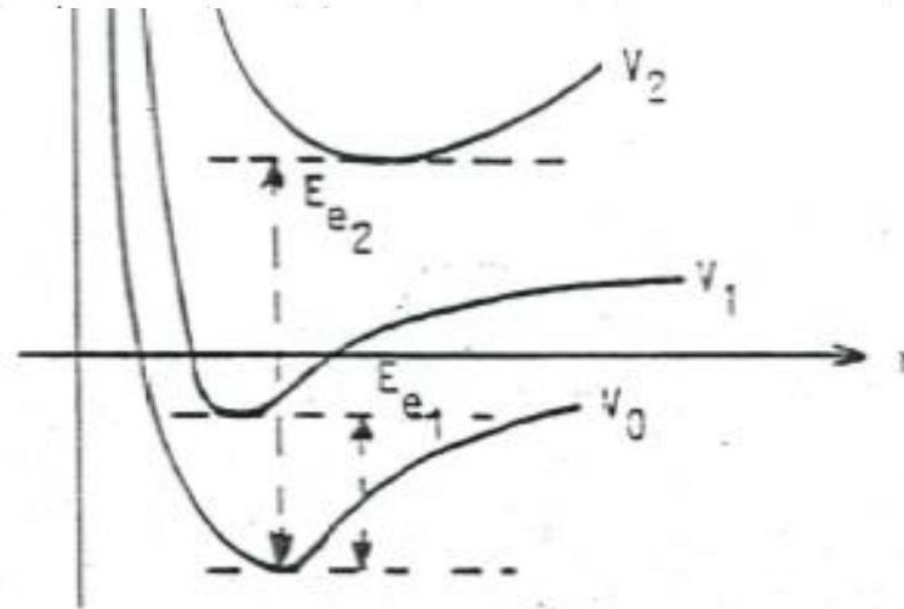
In which $H_{el} = T_e + V_{ee} + V_{ne}$

If all nuclei are fixed in space, then the coulomb energy associated with the repulsion of two nuclei (V_{nn}) is only a number which can be added to the electronic energy

$$U = E_{el} + V_{nn} \quad (7)$$

$$E^{el} = E^{el} \left(\underbrace{\vec{R}_1, \vec{R}_2, \dots}_{\text{géométrie nucléaire}} \right)$$

For a diatomic molecule



If the potential energy curves are well separated

$$E \sim E_e + E_v + E_r$$

Electron Motions

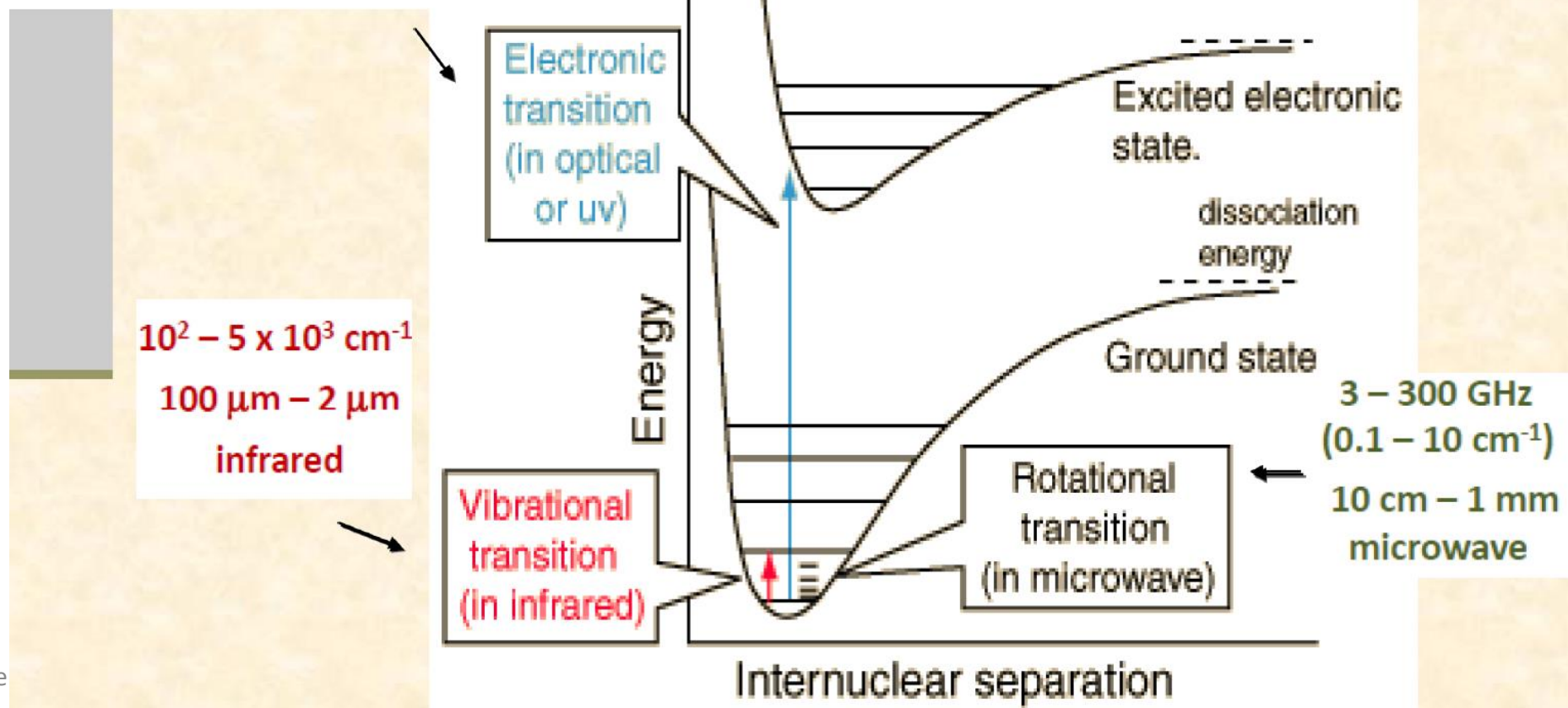
Nuclei motions

$$\Delta E \approx 2 \times 10^4 - 10^5 \text{ cm}^{-1}$$

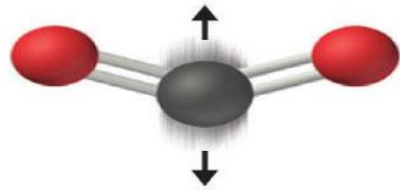
Transitions at $\lambda \approx$ 500 - 100 nm

Vis - UV

$$\Delta E_{el} \gg \Delta E_{vib} \gg \Delta E_{rot}$$



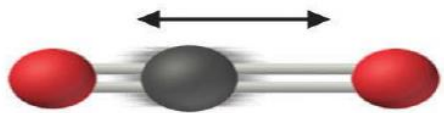
3 types of nuclear motions



bending

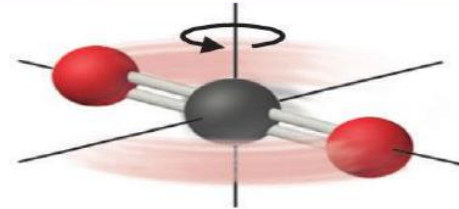


symmetric stretching

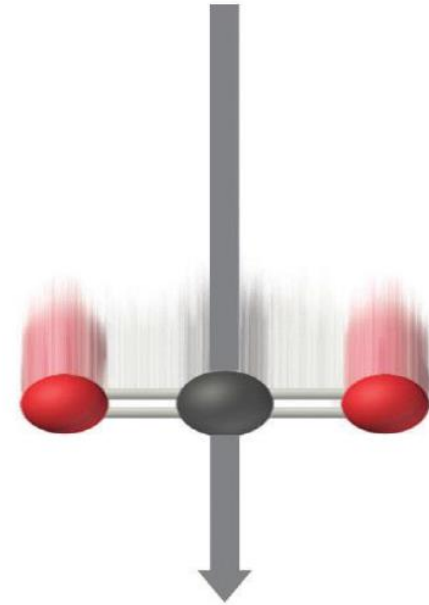
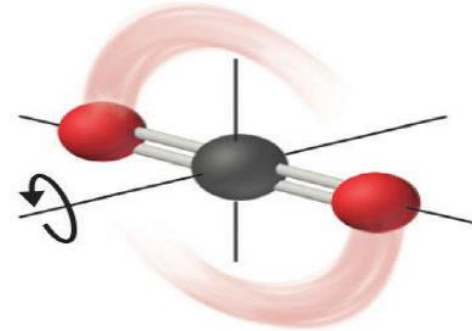


asymmetric stretching

vibrational motion



rotational motion



translational motion



Harmonic
Oscillator
model

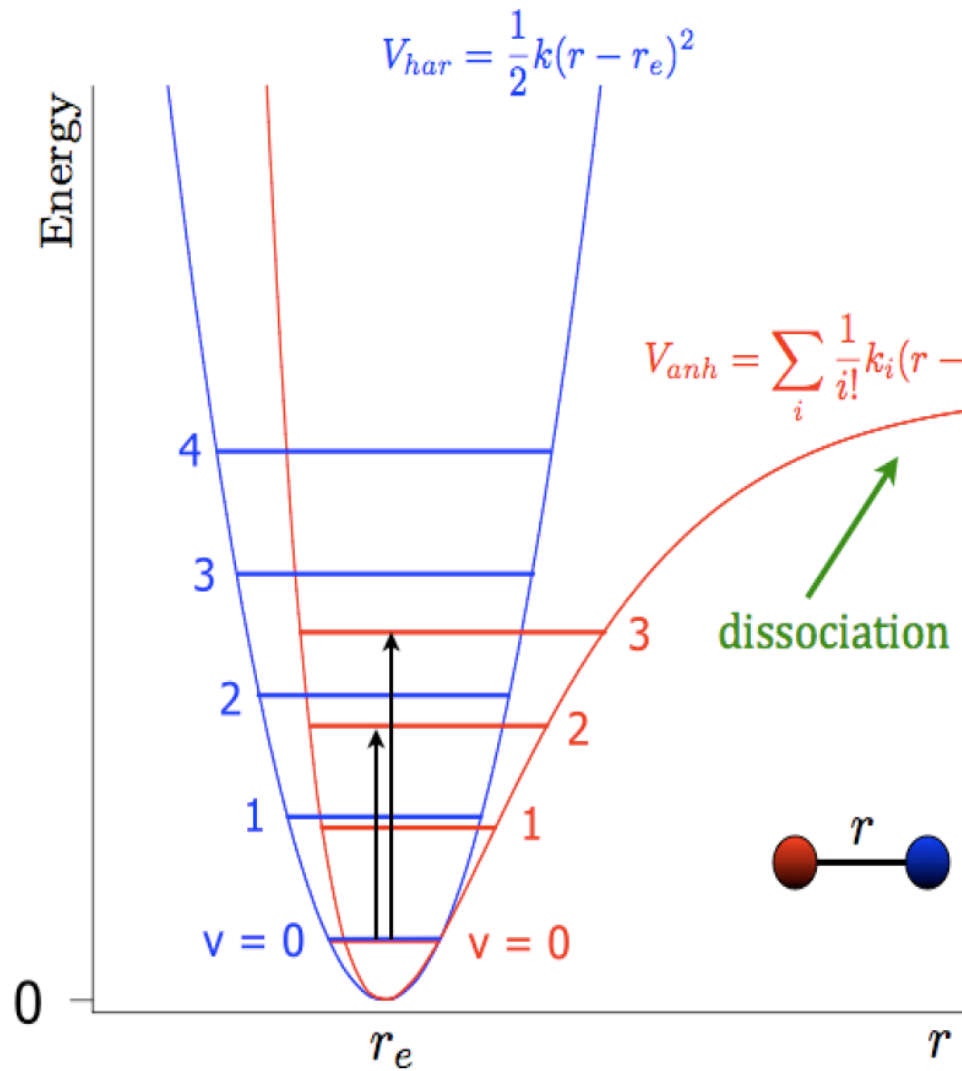


Rigid rotor
model



Can be separated
From the other motions
Energy = constante

Vibration: Harmonic and anharmonic oscillators



- Harmonic oscillator :

$$E_v = \omega_e(v + 1/2)$$

$$\omega_e = \frac{1}{2\pi c} \sqrt{k/\mu}$$

$k = \frac{d^2V}{dr^2}$

Reduced mass : $\frac{1}{\mu} = \frac{1}{m_1} + \frac{1}{m_2}$

- Anharmonic oscillator :

$$E_v = \omega_e(v + 1/2)$$

$$-\omega_e x_e (v + 1/2)^2 + \dots$$

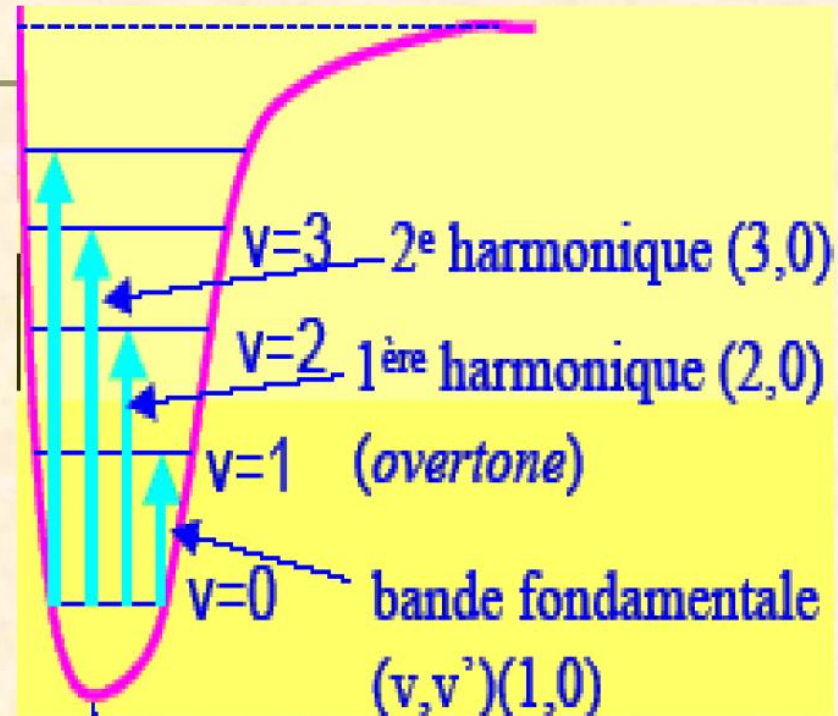
$$\omega_e x_e = -\frac{5 k_3^2}{48 \omega_e} + \frac{k_4}{16}$$

Force constants : $k_n = \frac{d^n V}{dr^n}$

On the IR spectrum, we observe :

* **Fundamental Bands:**
vibrations $v=0 \rightarrow v=1$

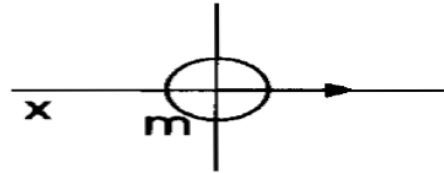
* **Overtone bands:**
multiples of fundamental
bands (Ex. $2v$)



- **Combination bands ($v_1 + v_2$ for example) :**
simultaneous excitation of several fundamental vibrations
- **Hot bands:** initial levels are not $v = 0$

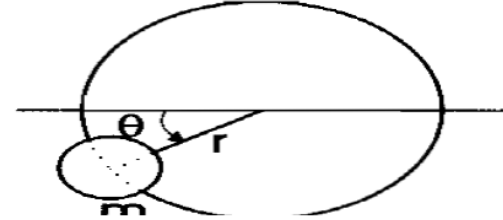
Moments of inertia, rotational angular momentum

Linear Motion



Linear Motion

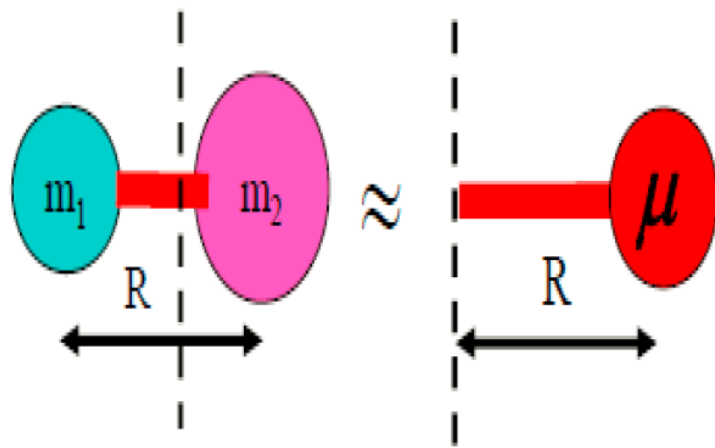
Angular Motion



Angular Motion

	<i>Position</i>	
Distance, x		Angle, θ
	<i>Velocity</i>	
Velocity, $v = \dot{x} = dx/dt$		Angular velocity, $\omega = \dot{\theta} = d\theta/dt$
	<i>Mass</i>	
Mass, m		Moment of inertia, $I = mr^2$
	<i>Momentum</i>	
Linear momentum, $p = mv$		Angular momentum, $J = I\omega$
	<i>Kinetic energy</i>	
$E_k = \frac{1}{2}mv^2 = p^2/2m$		$E_k = \frac{1}{2}I\omega^2 = J^2 / 2I$

Diatomic molecule



$$I = \sum_i m_i r_i^2 = m_1 r_1^2 + m_2 r_2^2 = \mu R^2$$

Where the

reduced mass,

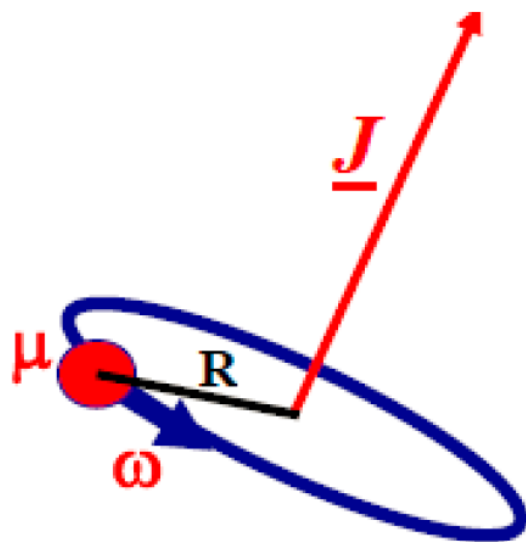
$$\mu = \frac{m_1 m_2}{(m_1 + m_2)}$$

Definition: The **moment of inertia** I of

centre of mass is given by;

$$I = \sum_i m_i r_i^2$$

where m_i is the mass of the i th particle and r_i is its perpendicular distance from the axis



The angular momentum,

$$J = I \omega \quad (\text{c.f. } p = mv)$$

The rotational kinetic energy,

$$E = J^2 / 2I = \frac{1}{2} I \omega^2$$

$$(\text{c.f. } E = p^2 / 2m = \frac{1}{2} mv^2)$$

From diatomics

to

polyatomic molecules

$$E = J^2/2I = \frac{1}{2} I \omega^2$$



$$\frac{1}{2} I_x \omega_x^2 + \frac{1}{2} I_y \omega_y^2 + \frac{1}{2} I_z \omega_z^2$$

$$J = I\omega$$

$$\begin{pmatrix} J_x \\ J_y \\ J_z \end{pmatrix} = \begin{pmatrix} I_{xx} & I_{xy} & I_{xz} \\ I_{yx} & I_{yy} & I_{yz} \\ I_{zx} & I_{zy} & I_{zz} \end{pmatrix} \begin{pmatrix} \omega_x \\ \omega_y \\ \omega_z \end{pmatrix}$$

Rotational energies: how to calculate them ?

$$H_0^{rot} (\text{energie}) = \frac{1}{2} I_x \omega_x^2 + \frac{1}{2} I_y \omega_y^2 + \frac{1}{2} I_z \omega_z^2$$

$$J = I\omega$$

$$= \frac{J_x^2}{2I_{xx}} + \frac{J_y^2}{2I_{yy}} + \frac{J_z^2}{2I_{zz}} \longrightarrow = J_x^2 B_x + J_y^2 B_y + J_z^2 B_z$$

Rotational constants

$$B = \frac{h}{8\pi^2 I} = \frac{505379.07}{I(\text{amu}\text{\AA}^2)} \text{MHz} \quad B = \frac{h}{8\pi^2 cI} = \frac{16.8576314}{I(\text{amu}\text{\AA}^2)} \text{cm}^{-1}$$

$$B (\text{in Joule}) = \frac{\hbar^2}{2I}$$

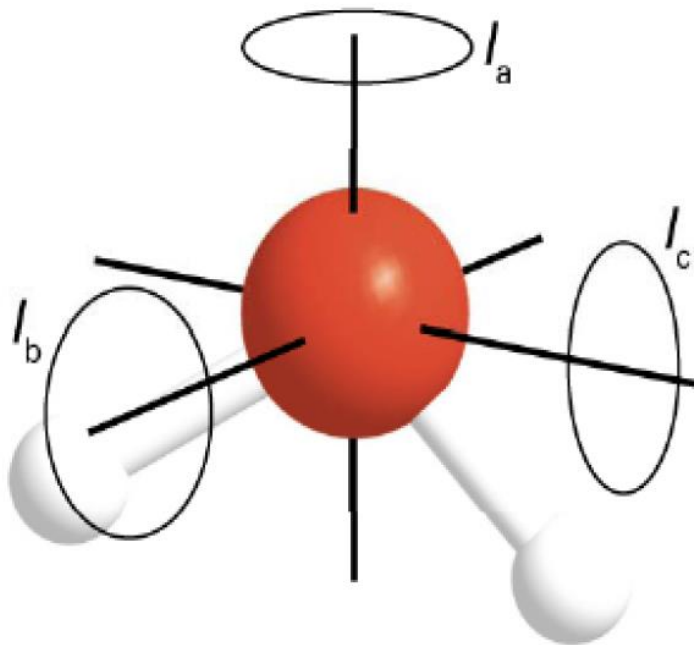
Rotational constants are related to molecular structure

For diatomics we defined a rotational constant $\tilde{B} \propto \frac{1}{I} = \frac{1}{\mu R^2}$

In general we require three such rotational constants:

as wavenumbers: $\tilde{A} = \frac{h}{8\pi^2 c I_a}$ $\tilde{B} = \frac{h}{8\pi^2 c I_b}$ $\tilde{C} = \frac{h}{8\pi^2 c I_c}$

$$\tilde{A} \geq \tilde{B} \geq \tilde{C}$$



H₂O molecule

$$\tilde{A} = 27.9 \text{ cm}^{-1}$$

$$\tilde{B} = 14.5 \text{ cm}^{-1}$$

$$\tilde{C} = 9.3 \text{ cm}^{-1}$$

But, we can no longer relate these constants explicitly to individual bond lengths within the molecule.

Schrödinger equation rigid rotors

$$\hat{H}\psi_r = E_r\psi_r$$

Rotational operators

$$\nearrow \mathbf{J}^2 |\Psi_r\rangle = \mathbf{J}(\mathbf{J}+1) |\Psi_r\rangle$$

$$\searrow \mathbf{J}_z |\Psi_r\rangle = \mathbf{K} |\Psi_r\rangle$$

***J** and **K** are the quantum numbers for rotation*

$$(J = 0 \rightarrow \infty)$$

$$J = 0, 1, 2, \dots$$

repérer la molécule dans le système d'axes

Rotational energies for diatomic or linear molecules

$$E_J = BJ(J+1)$$

- J is the rotation quantum number = 0, 1, 2, ...
- B is the rotational constant

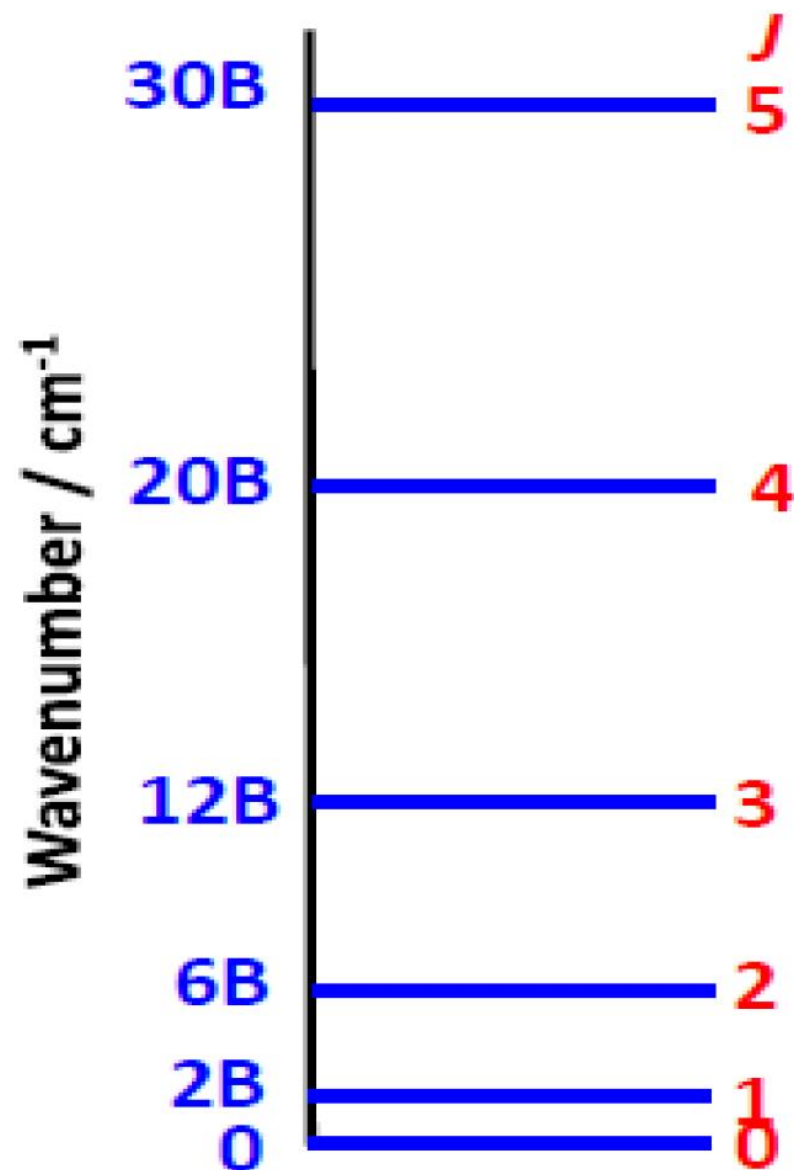
$$B \text{ (in Joule)} = \frac{\hbar^2}{2I}$$

We can also give the B in cm^{-1}

$$F_J = \frac{E_J}{hc} = \tilde{B}J(J+1)$$

$$\tilde{B} = \frac{h}{8\pi^2 cI} = \frac{h}{8\pi^2 c\mu R^2}$$

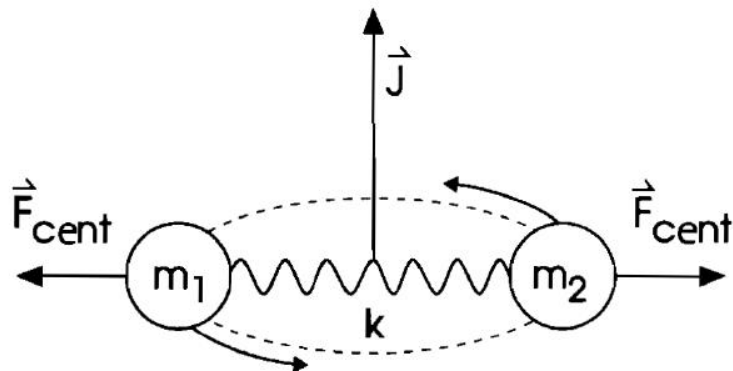
	\tilde{B}
H ₂	60.85 cm^{-1}
CO	1.93 cm^{-1}
HCl	10.59 cm^{-1}



Centrifugal distortion

The bonds between the atoms are not really rigid, the centrifugal force imposed to the atoms is susceptible to increase the bond length.

if J increases, the molecule turns faster, the centrifugal force increases, which **increases the bond length**, r , and thus the moment of inertia increases, since $I = m r^2$.



$$B = \frac{h}{8\pi^2 c I}$$

This increase of I implies **a decrease of B**

Centrifugal distortion

$$E(v, J) = hc [G(v) + F(J)]$$

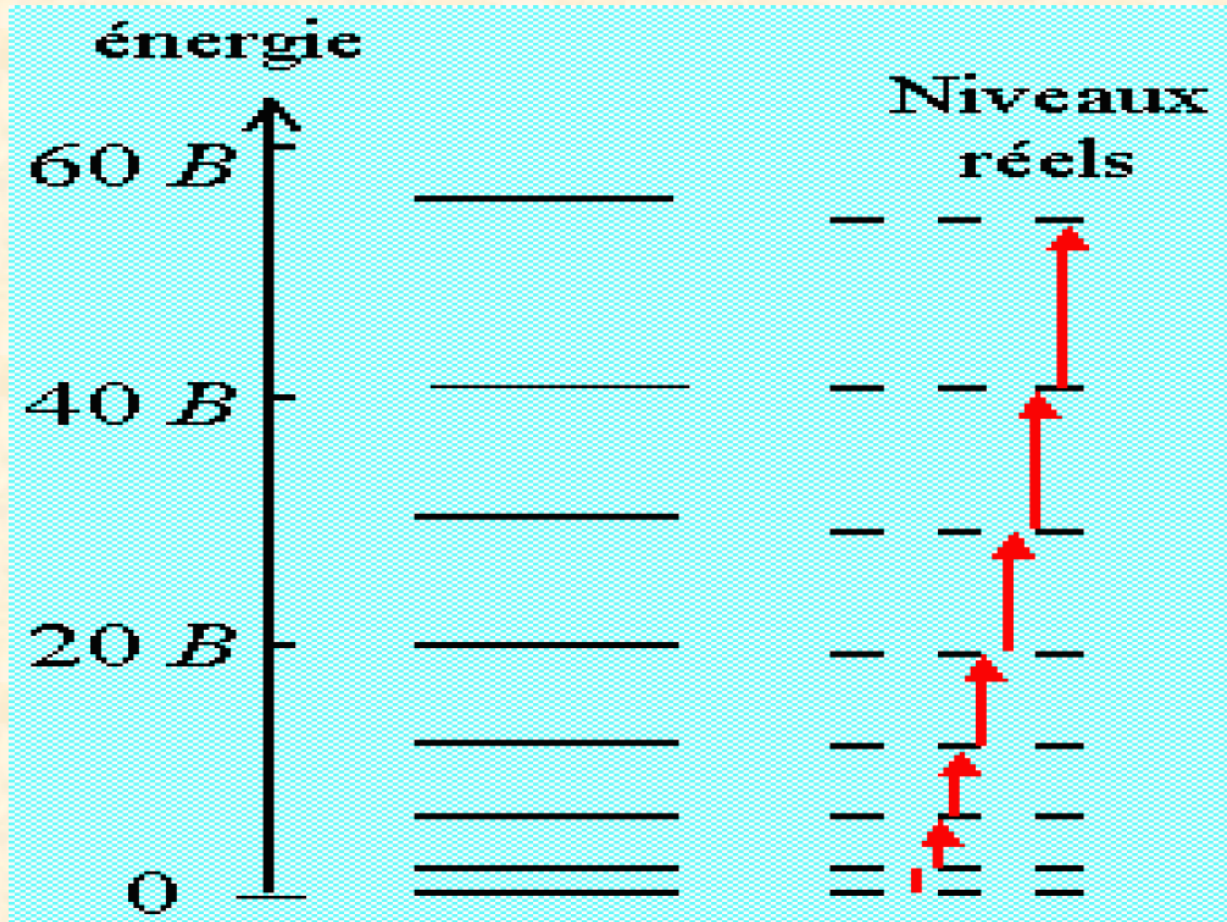
The energy of the vibrating-rotating molecule is :

$$G(v) + F(J) = \omega_e (v + 1/2) - \omega_e x_e (v + 1/2)^2 \\ + B J (J + 1) \\ - D J^2 (J + 1)^2 - \dots$$

The D parameter is centrifugal distortion

Whereas $\omega_e x_e$ is
related to the anharmonicity of the vibration

Centrifugal distortion effect on the energy levels



Diatomic molecules

$J \rightarrow J'=J-1$: P Branch

$J=0 \rightarrow J'=0$: Q branch
« forbidden » transition

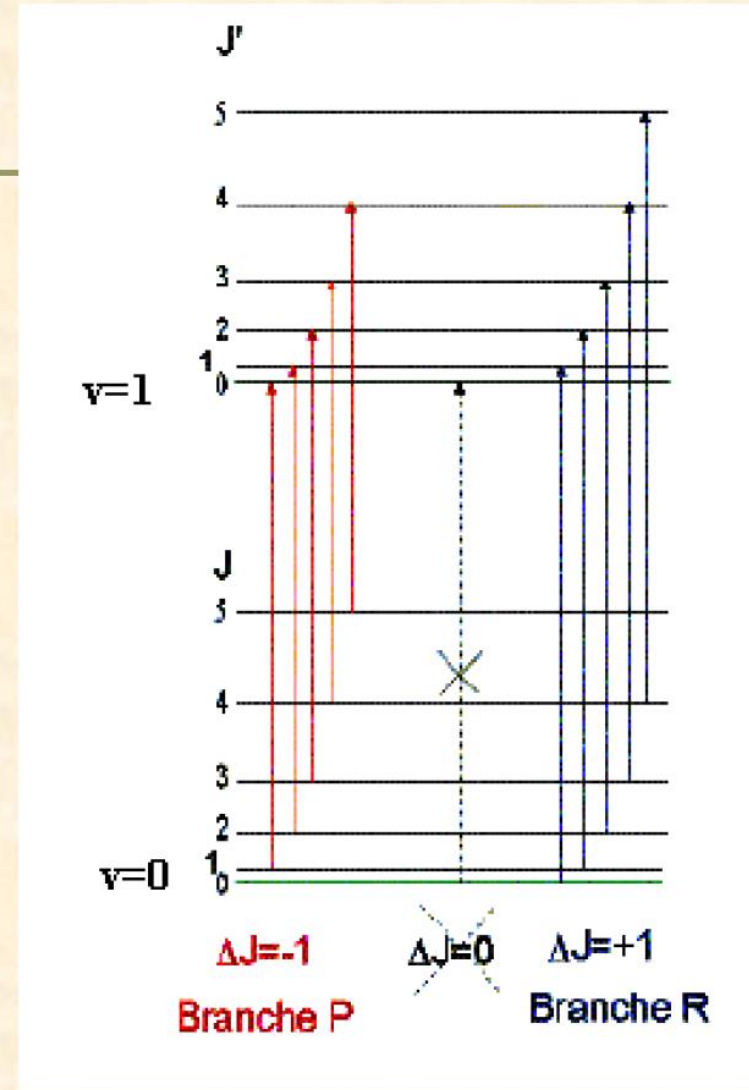
$J \rightarrow J'=J+1$: R Branch

a) $\Delta v = 0$; $\Delta J = \pm 1$: pure rotation spectrum (microwave).

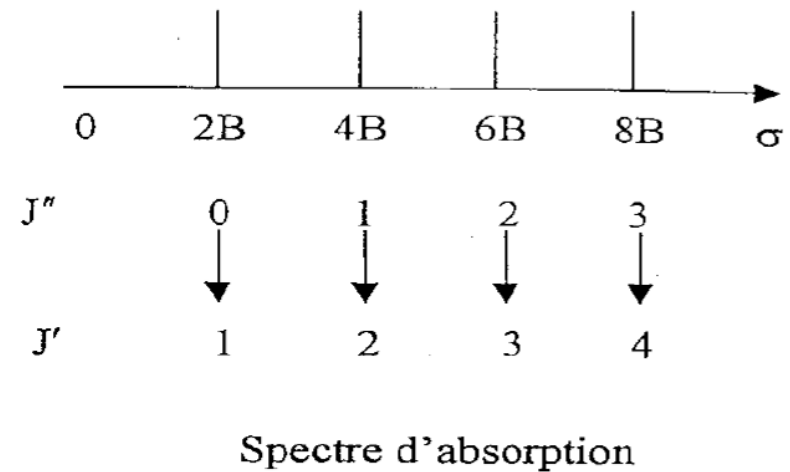
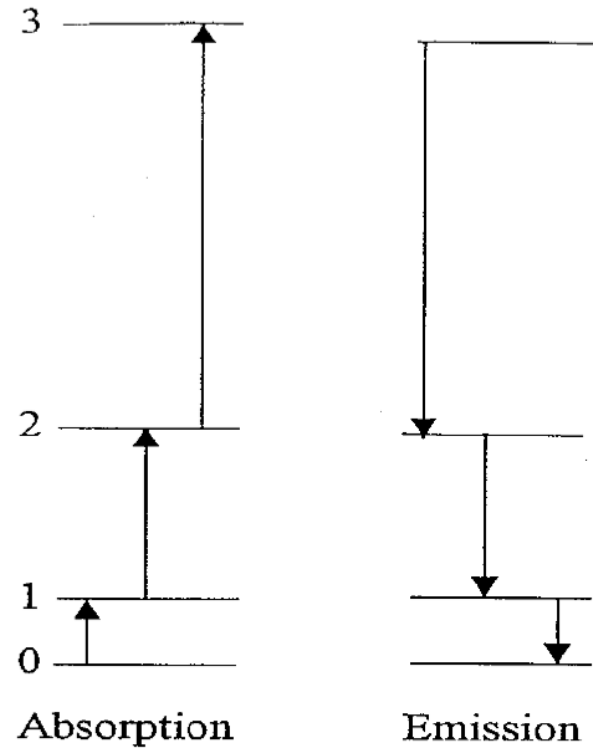
The molecule must have a permanent dipolar moment

b) $\Delta v = \pm 1$; $\Delta J = \pm 1$: vibration-torsion (infrared)

The dipole moment must change during the vibration



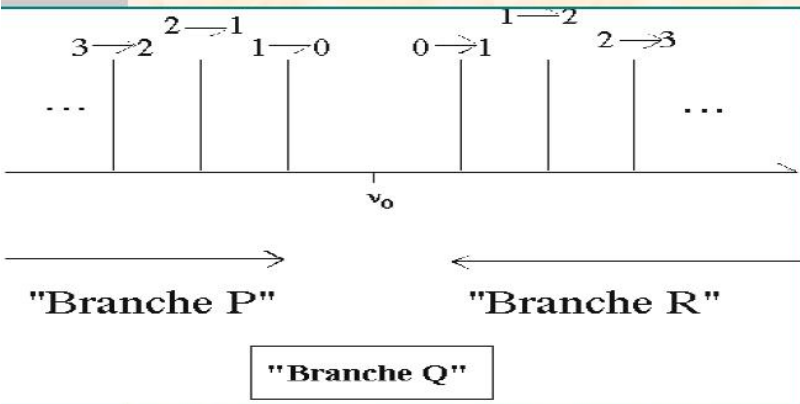
Pure rotation spectrum (microwave) for a diatomic molecule



The heavier the molecule is , the closer the lines are

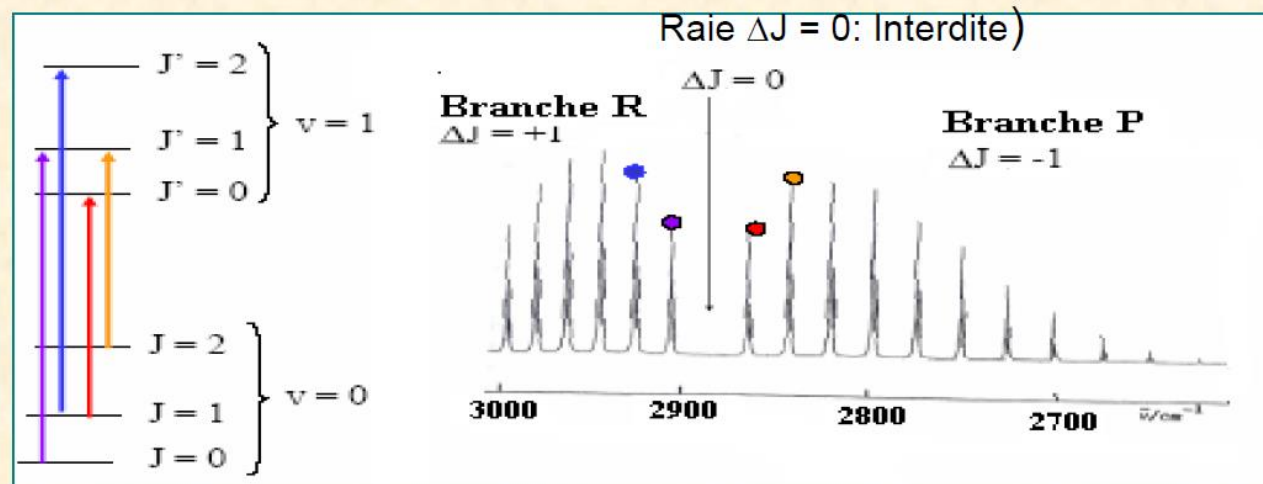
B) rotation-vibration spectrum

- Vibration-rotation transitions lead to a series of lines



R Branch : at higher frequencies ν relative to the band center ν_0

- Like for pure rotation spectra, **intensities** depend on the level population (**function of J**)



What about polyatomic molecules???

- **Classification** of the molecules

- *Linear* molecules : $I_a = 0, I_b = I_c$ (CO_2, HCN)

- *Spherical* tops : $I_a = I_b = I_c$ (CH_4, SF_6)

- *Prolate symmetric* tops : $I_a < I_b = I_c$ ($\text{CH}_3\text{Cl}, \text{C}_2\text{H}_6$)

- *Oblate symmetric* tops : $I_a = I_b < I_c$ ($\text{CCl}_3\text{H}, \text{BF}_3$)

- *Asymmetric* tops : $I_a < I_b < I_c$ ($\text{H}_2\text{O}, \text{HNO}_3, \text{HCOOH}$)

Concept of normal vibrations - fundamentals

Polyatomic molecules : N atoms $\Rightarrow 3N$ motions

Suppressing the motions equivalent to translations $\Rightarrow 3N-5$ or 6 vibrations

Matrix of motions transformed to eigenvalues \Rightarrow fundamental vibrations

Number of fundamentals $< 3N-5$ as degenerate vibrations related to the symmetry of the molecule

Symmetries

- Symmetry elements and operations
 - Plane of symmetry (σ)
 - Center of symmetry (i)
 - P-fold axis of symmetry C_p with $p=1,2,3\dots$
 - P-fold rotation-reflection axis S_p (rotation C_p + symmetry)
- Point groups

The combination of the symmetry elements (+ identity) forms a group structure and characterize the molecular structure relevant to the vibrational fundamentals

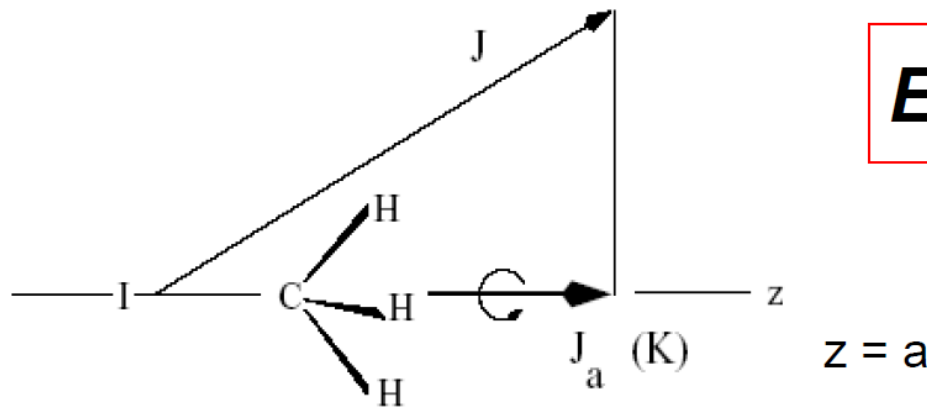
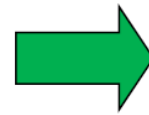
There are two types of symmetric rotors:

$$1) B_x = B_y \neq B_z$$

- A) *Prolate symmetric rotors* (“cigar” molecules)

- I_{zz} is defined as the smallest inertia moment and corresponds to the « A » rotational constant (which is always the biggest)

$$A = B_z, B = B_x = B_y$$



$$E_0^{rot} = B J(J+1) + (A-B) K^2$$

K is called K_a for prolate tops

Second type of symmetric tops

$$2) B_x = B_y \neq B_z$$

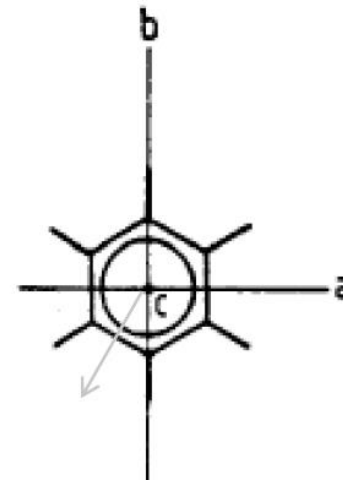
-B) *Oblate symmetric tops* (“plate” molecule):

I_{zz} is defined for those oblate tops as the biggest moment of inertia and correspond to the C rotational constant (which is the smallest constant)

$$B_x = B_y = B, C = B_z$$

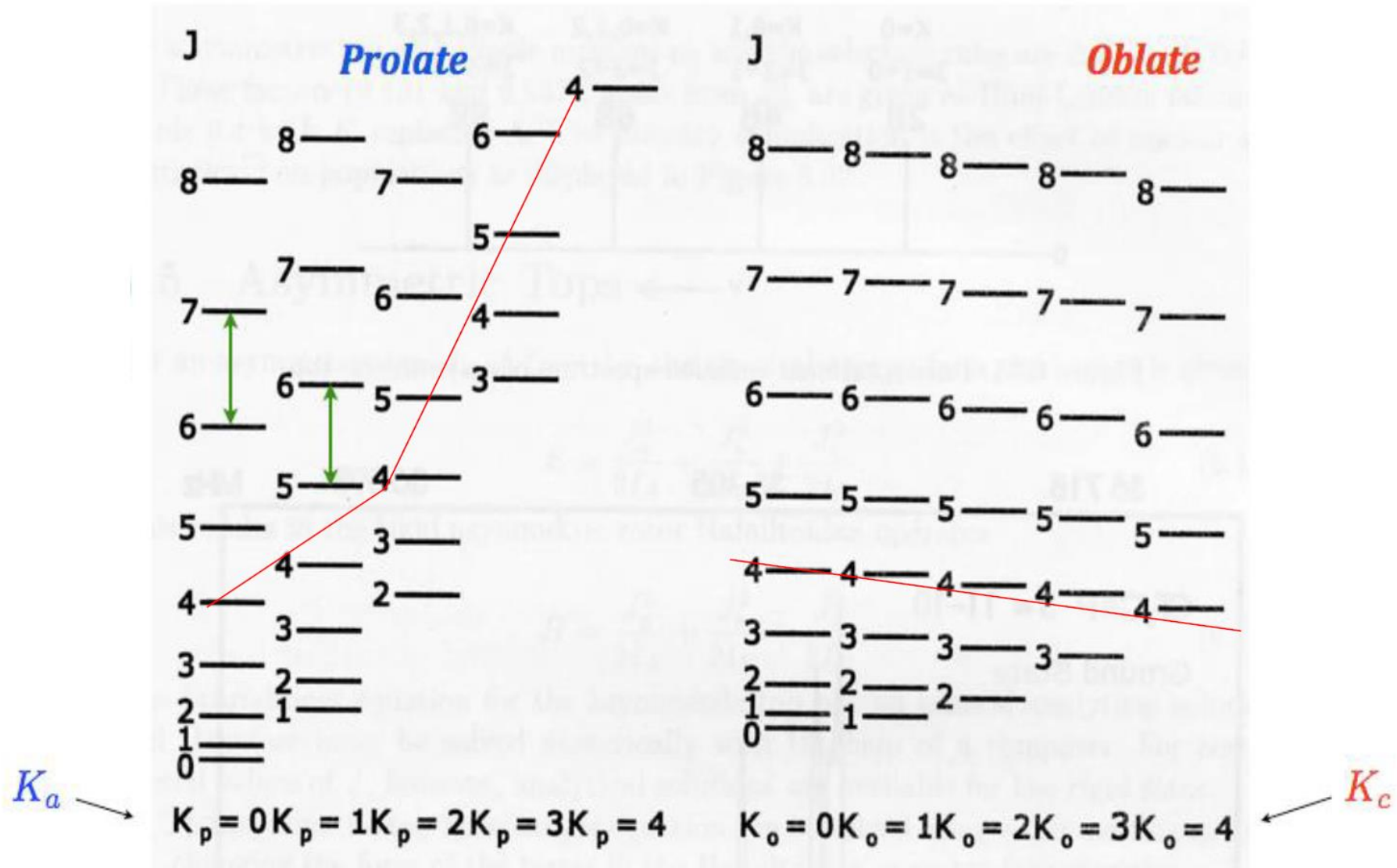
$$E_0^{rot} = BJ(J+1) + (C-B) K^2$$

K is called K_c for oblate tops



Rotation energies for symmetric tops

$$A \geq B \geq C$$



$$E_r(J, K) = BJ(J + 1) + \frac{(A - B)K^2}{> 0}$$

$$E_r(J, K) = BJ(J + 1) + \frac{(C - B)K^2}{< 0}$$

Molécules toupies symétriques

Rotation-vibration: transitions are induced by the variations of the **z component of dipole moment parallel** to the symmetry axis or by the **x et y components perpendicular** to this axis.

2 types of selection rules and 2 types of bands

■ **Parallel Band** (induced by the variations de μ_z)

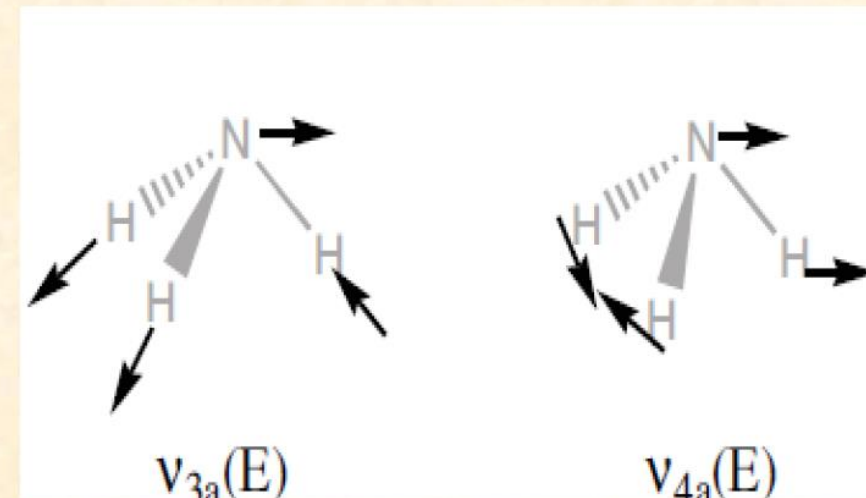
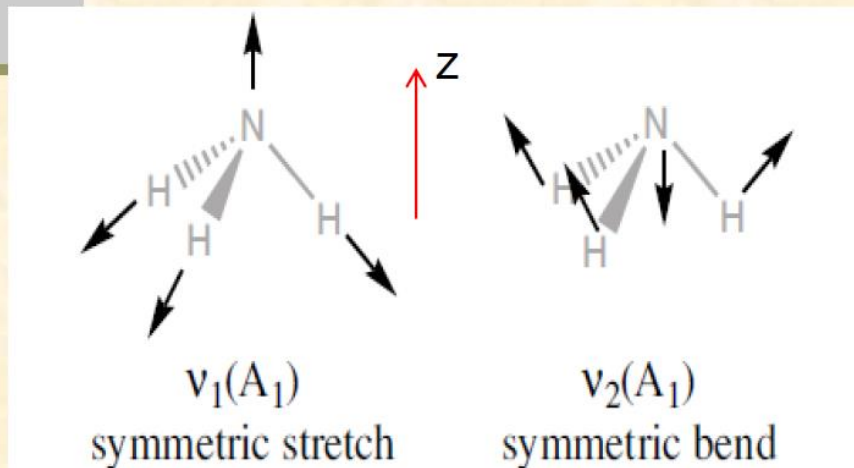
$$\Delta l = 0$$

- si $K \neq 0$ $\Delta J = 0, \pm 1$ et $\Delta K = 0$
- si $K = 0$ $\Delta J = \pm 1$ et $\Delta K = 0$

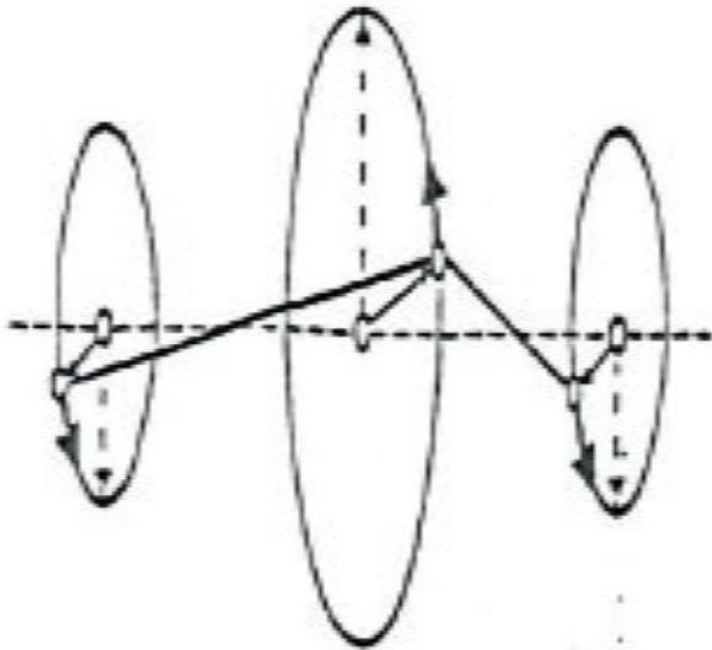
■ **Perpendicular Band** (induced by μ_x, μ_y)

$$\Delta l = \pm 1$$

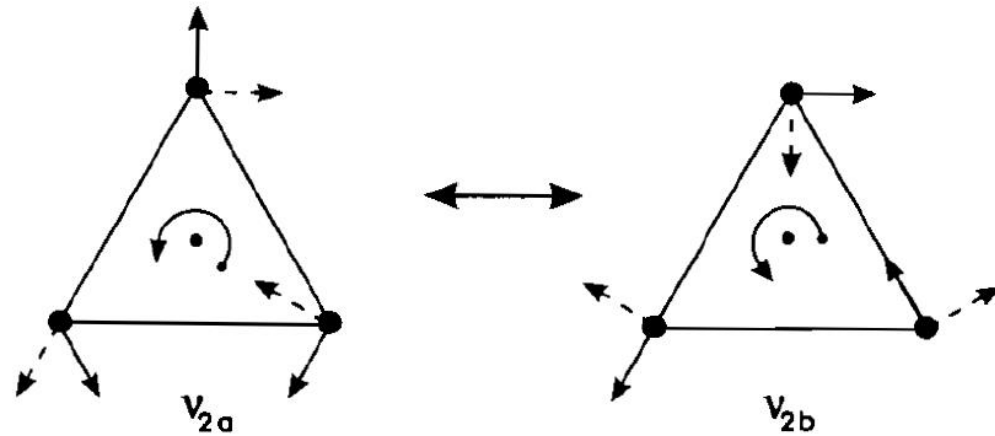
$$\Delta J = 0, \pm 1 \text{ et } \Delta K = \pm 1$$



What is happening in so-called « degenerate » modes?



Linear molecule (CO_2)



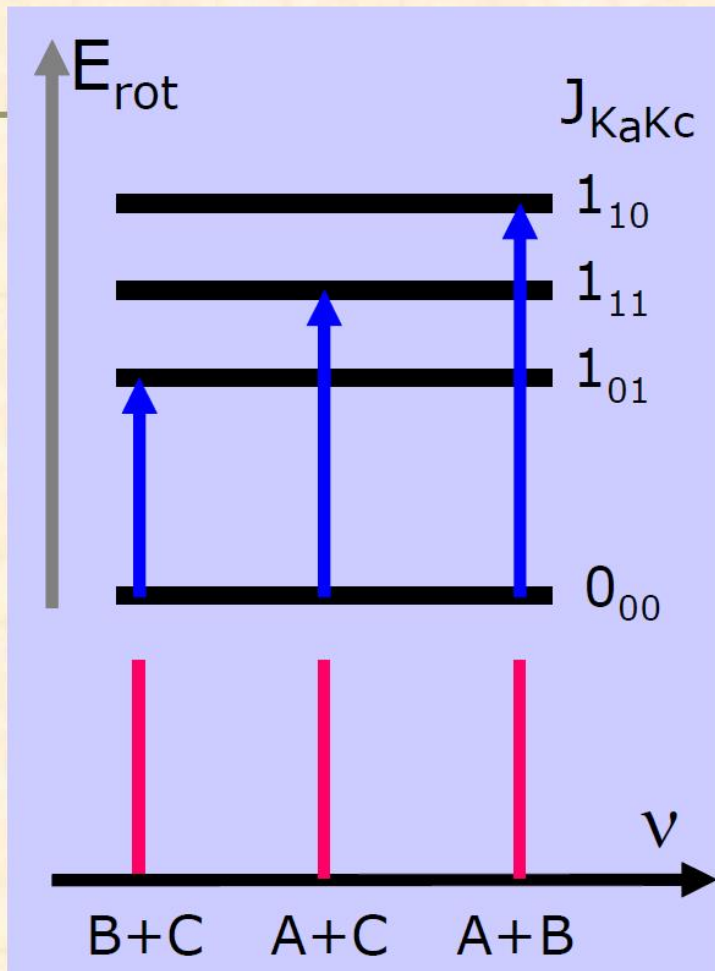
Symmetric top (H_3^+)

Rotational energy levels and transitions

Rigid rotor
(zero order energy)

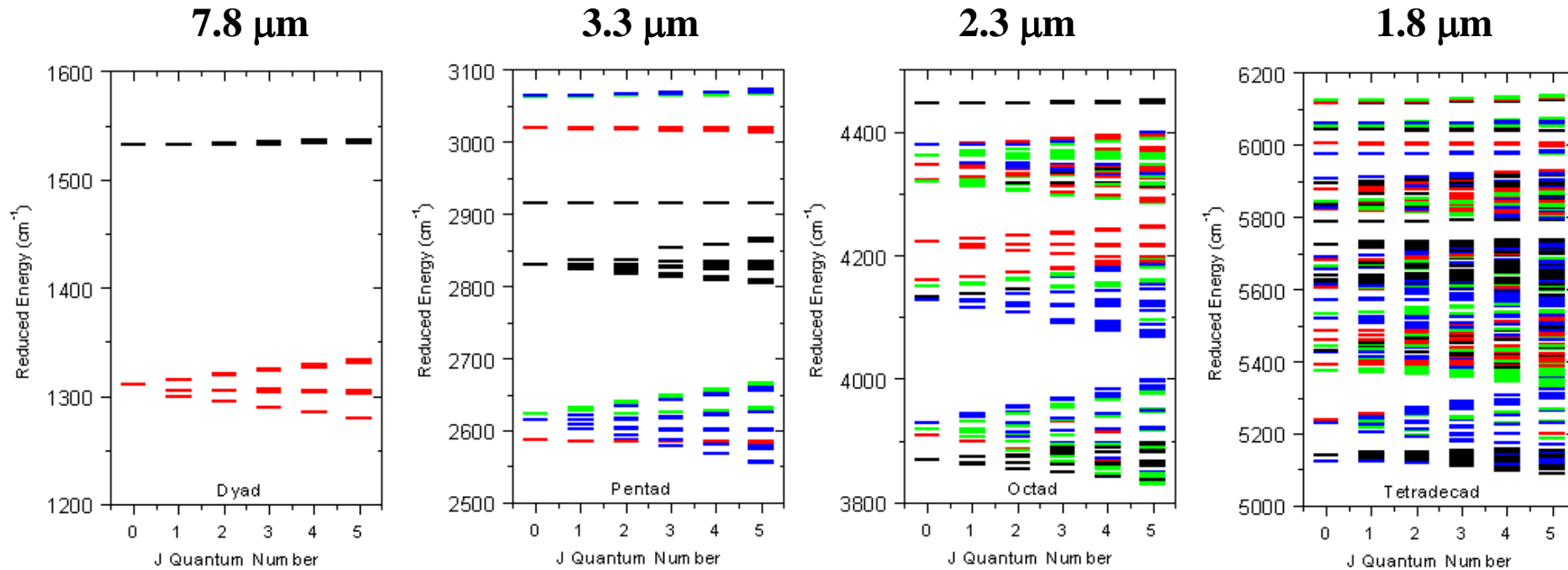
Asymmetric top, rotation characterized by the quantum numbers : J, K_a, K_c

Line Intensities : Depend on the Electric dipole moment $\mu (\mu_a, \mu_b, \mu_c)$



Limitation of the size of the molecule measured by most of Fourier-Transform spectrometers (2-20 GHz) : 250-300 μm

CH₄ : vibration/rotation bands



Dyad

2 vibrational states
2 sublevels

Pentad

5 vibrational states
9 sublevels

Octad

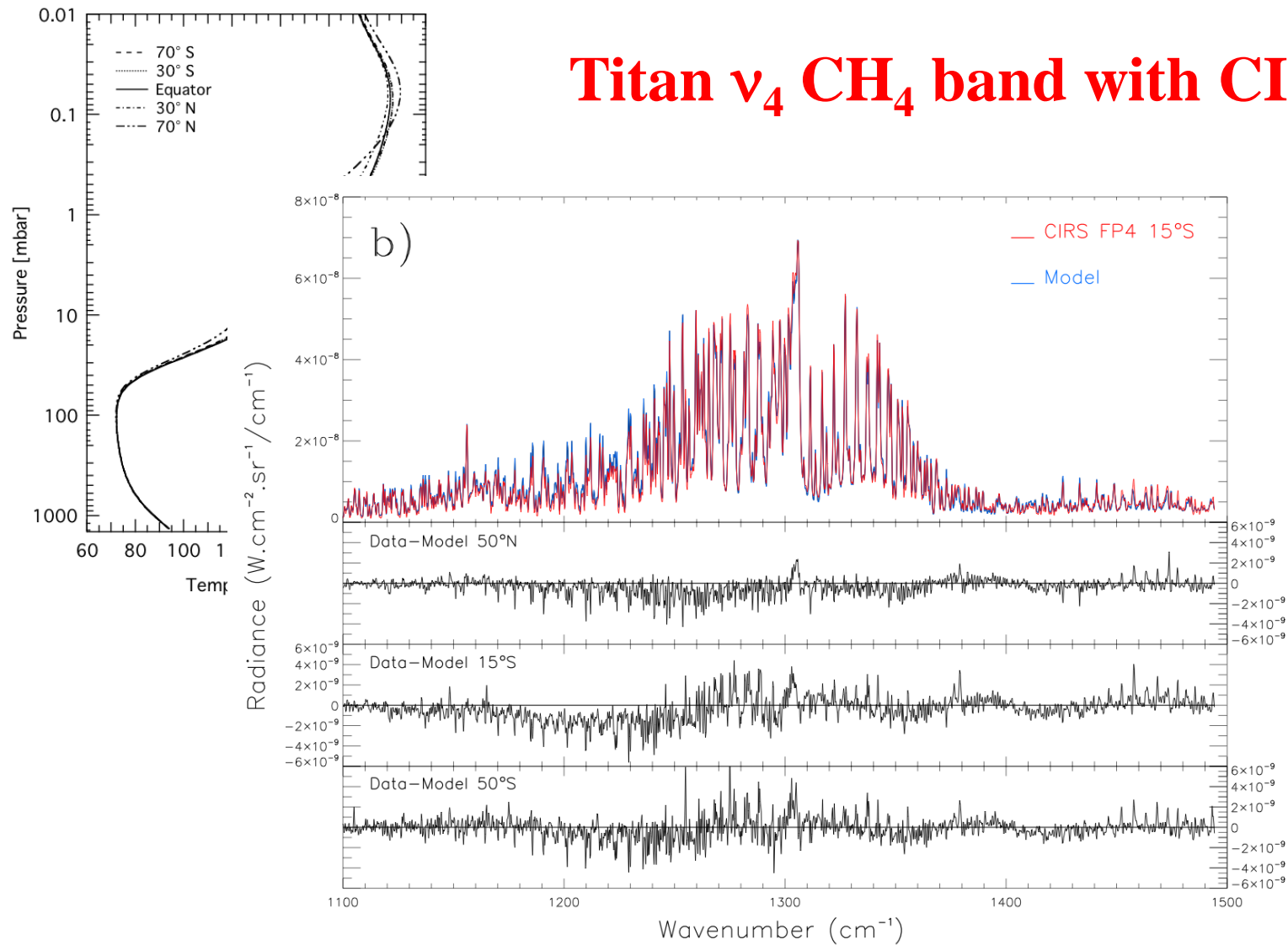
8 vibrational states
20 sublevels

Tetradecad

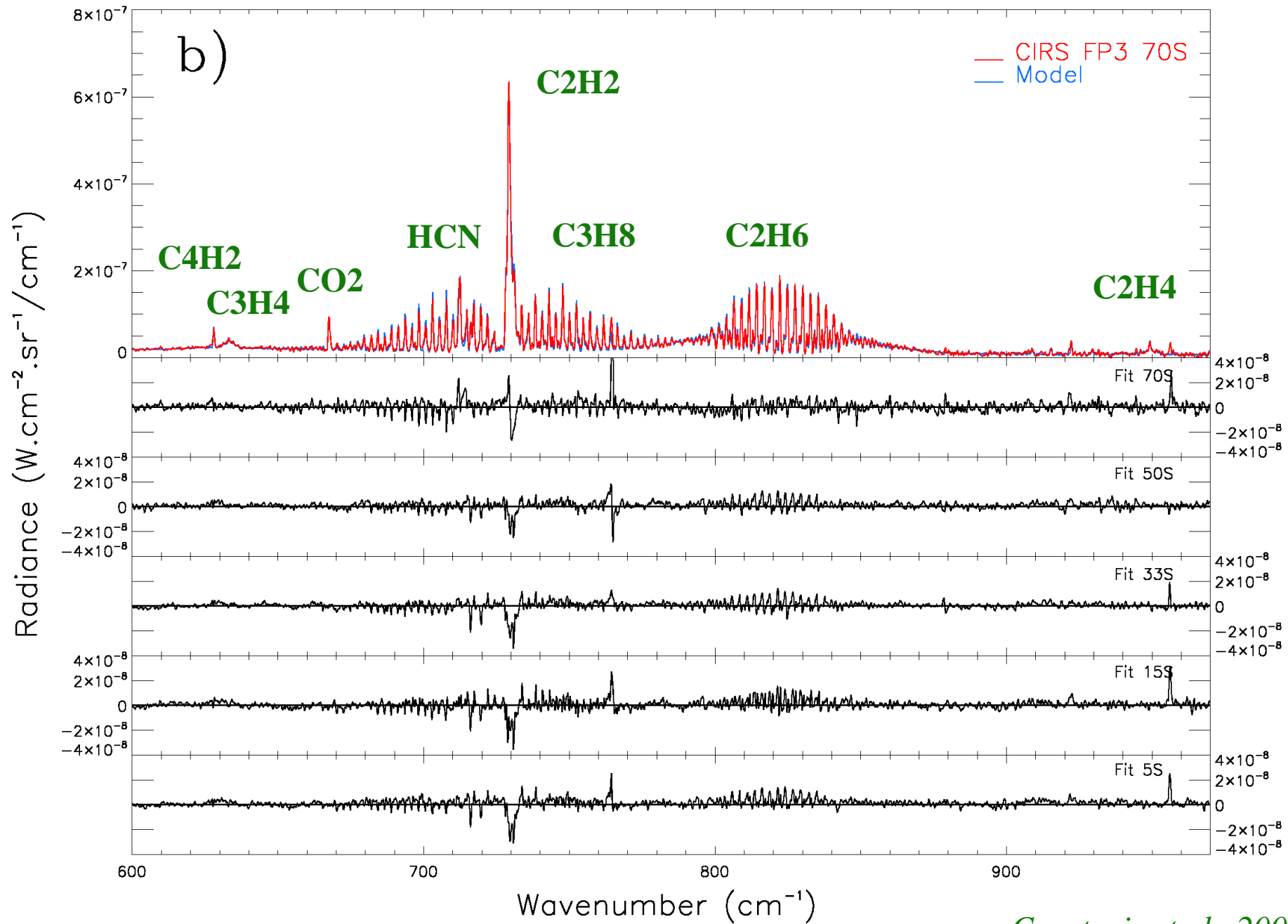
14 vibrational states
60 sublevels

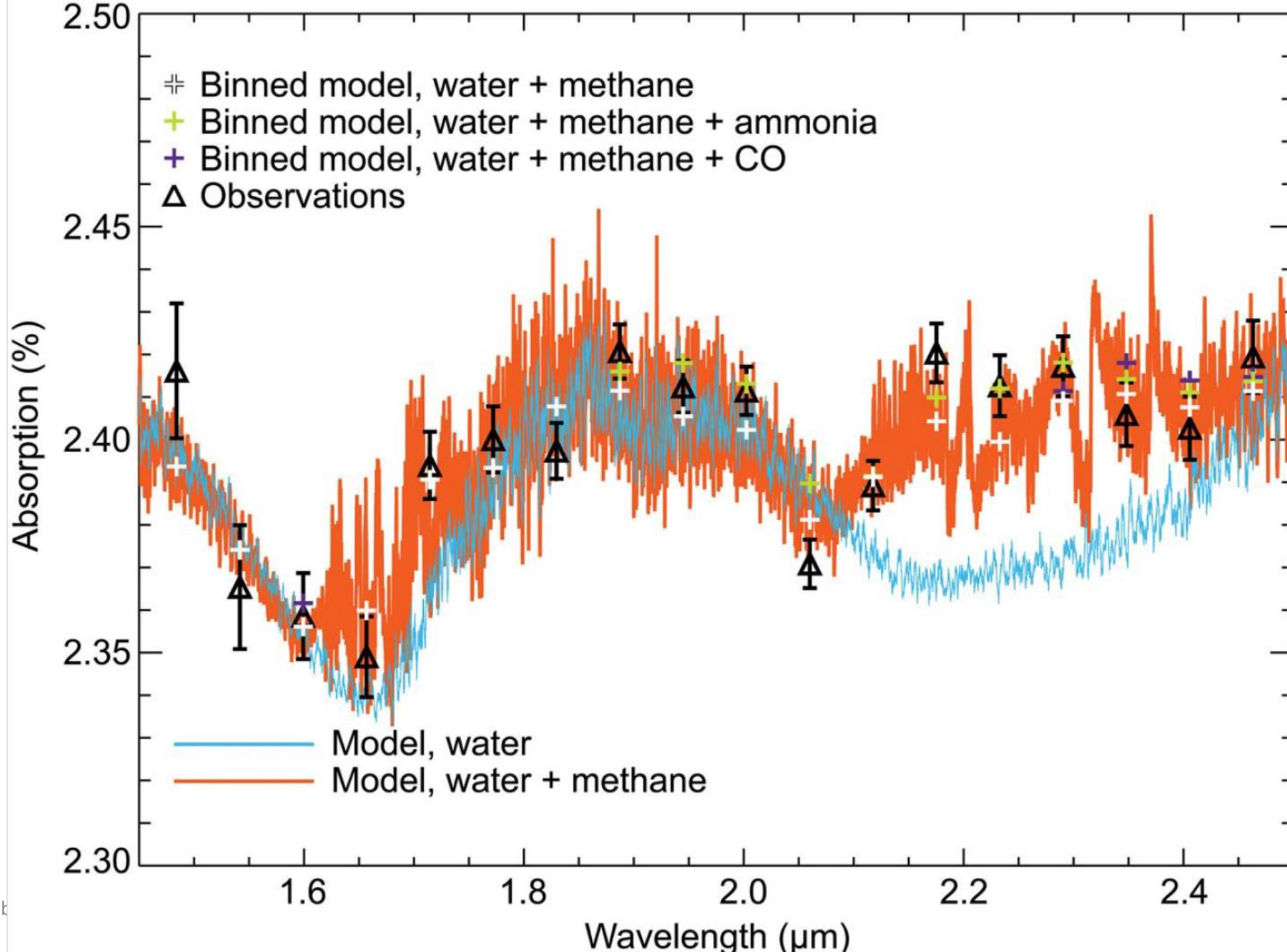


Titan ν_4 CH₄ band with CIRS



Coustenis et al., 2007





Additional complexities : internal motions

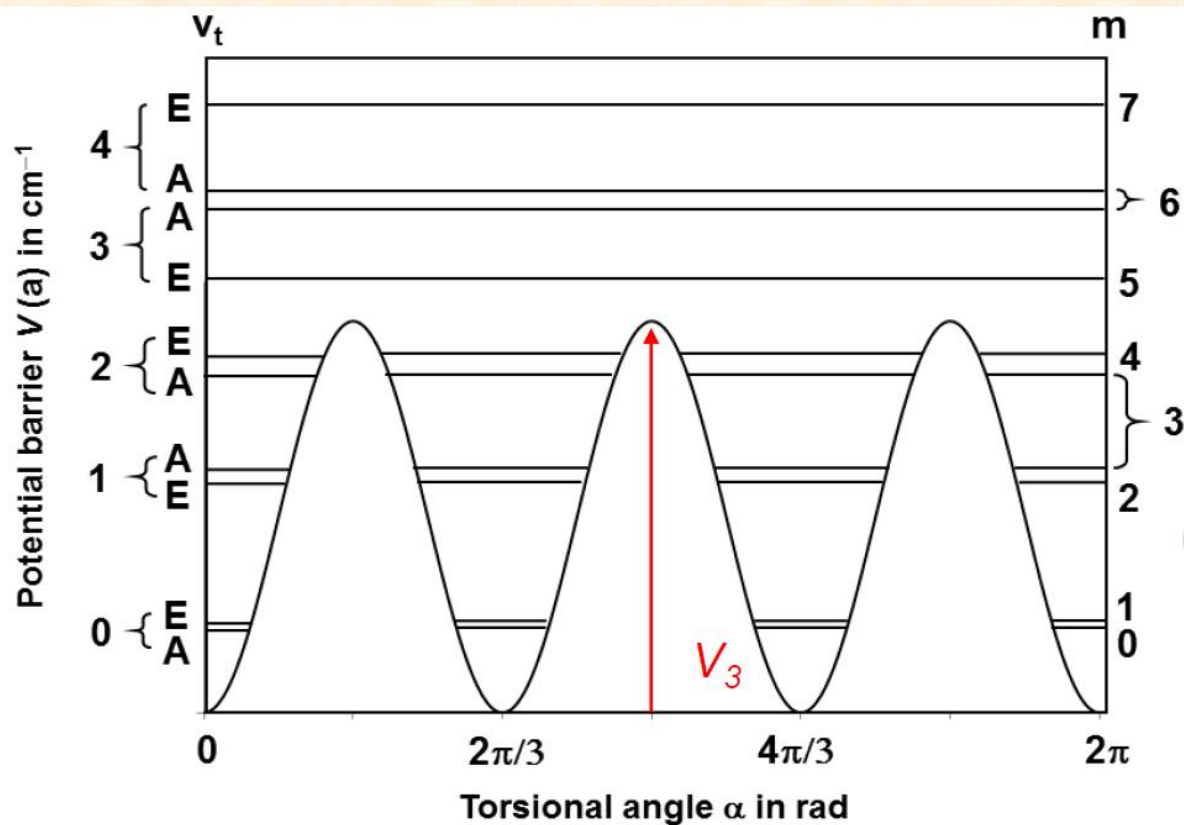
Internal motions in some molecules greatly complexify the spectroscopy.

Examples :

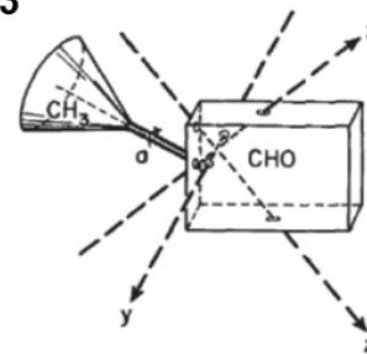
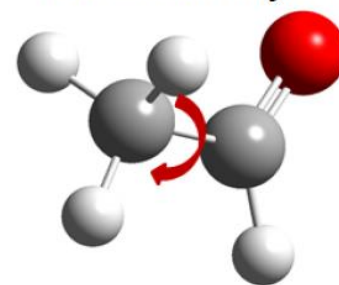
CH₃-COH (formaldehyde)

NH₃

Internal rotation



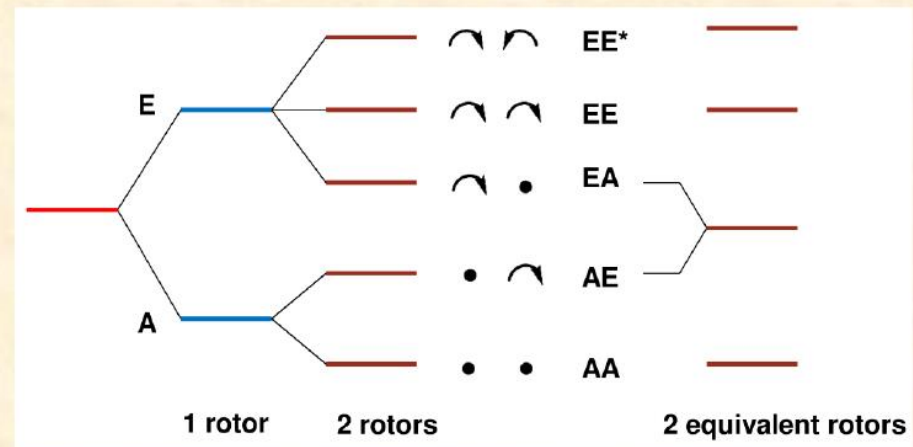
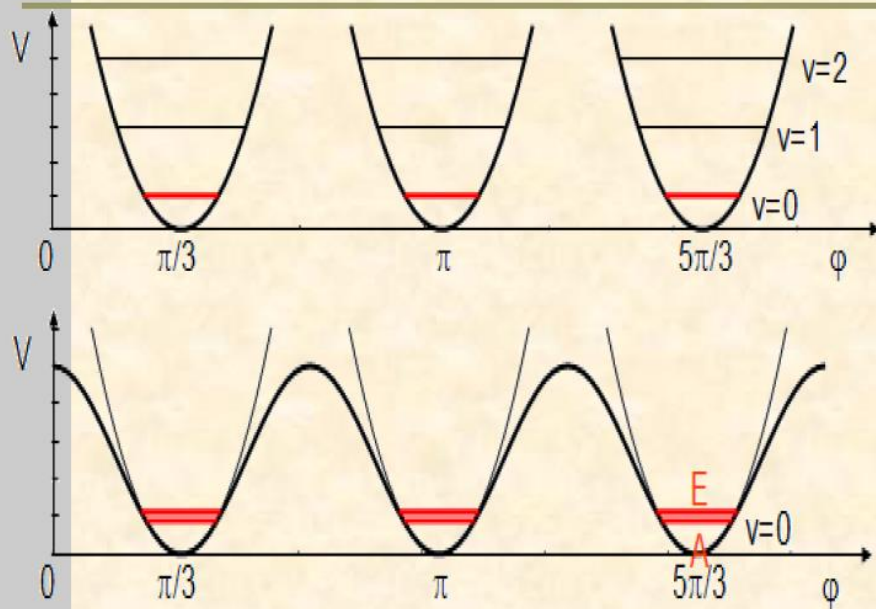
Acetaldehyde



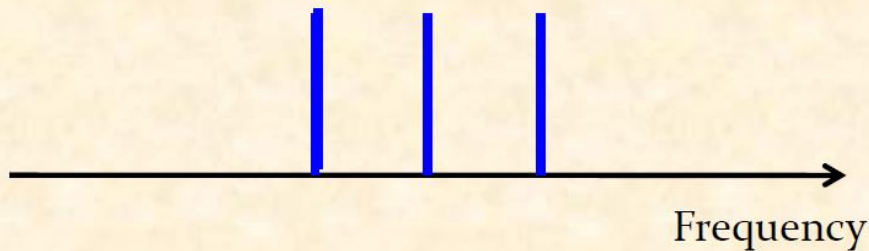
$$V(\alpha) = \frac{V_3}{2}(1 - \cos 3\alpha) + \frac{V_6}{2}(1 - \cos 6\alpha) + \dots$$

Lin and Swalen
Rev. Mod. Phys
1959

Internal rotation



AA AAE EA EE EE*

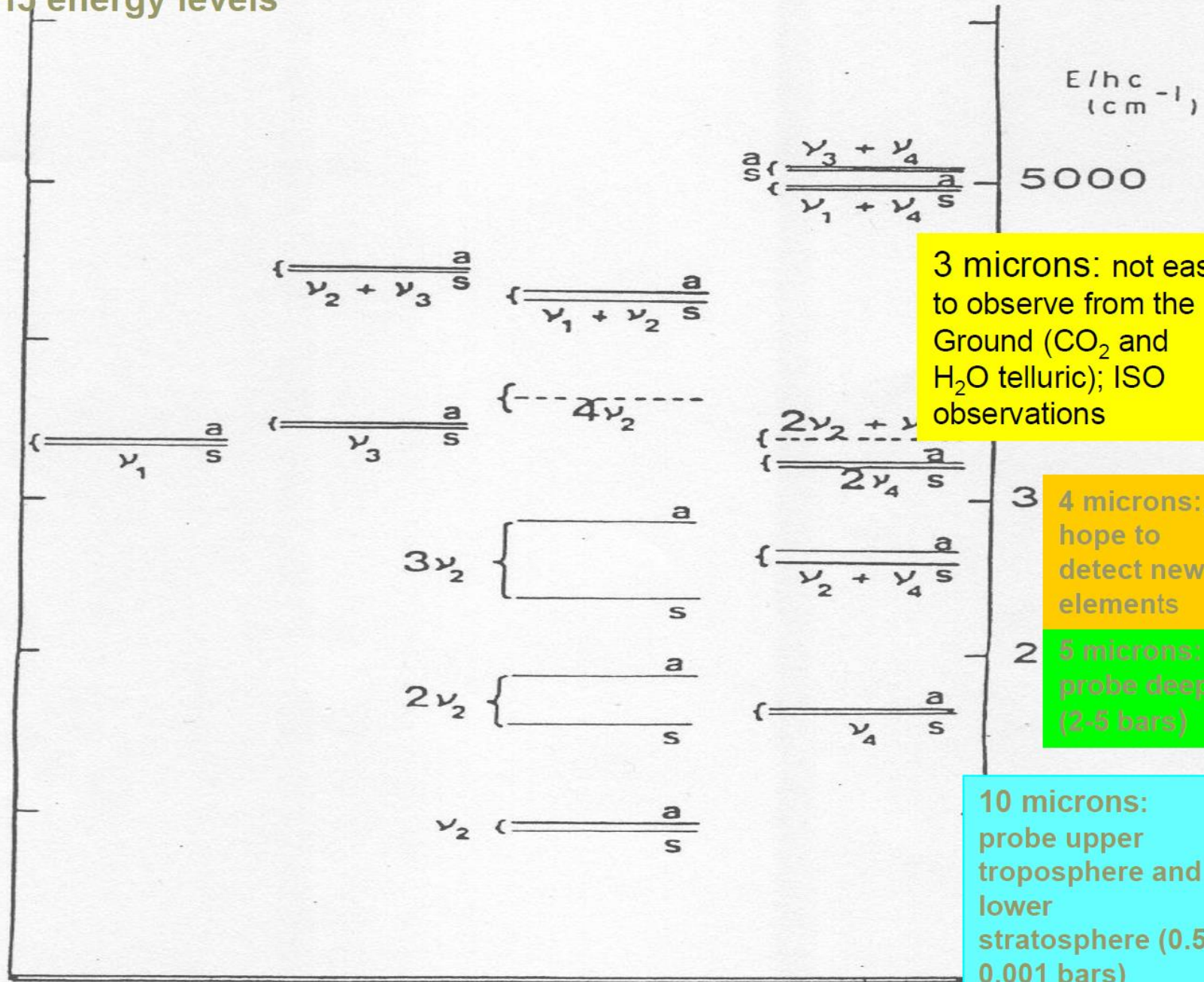


What do we know about the spectroscopy of ammonia NH₃ ?

,Range	Bands (cm ⁻¹)	Intensity cm ⁻² atm ⁻¹ at 296K	Position RMS (cm ⁻¹)	Intensities RMS (%)	Ref	
local modes						
4800-18000			3.3		Coy and Lehmann, 1989	
1626-18000			5.5		Kauppi and Halonen, 1995	
normal modes						
7600-8000						
6400-6800	$\nu_1+\nu_3, 2\nu_3$	10.?			Lundsberg-Nielsen et al, 1993 Xu et al 2003, Orphal 2006	
5900-6200						
4750-5150	$\nu_1+\nu_4/\nu_3+\nu_4$	17.			Brown and Margolis, 1996	
4200-4700	$\nu_2+\nu_3/\nu_1+\nu_2$	22.	0.2		Urban et al 1989	
3100-3700	$\nu_1/\nu_3/2\nu_4$	38.	0.085	9	Kleiner et al, 1999	3 microns
2200-3100	$3\nu_2/\nu_2+\nu_4$ +hot bands	1.	0.0069	6	Kleiner et al 1995 Cottaz et al 2001	4 microns
1300-2000	$2\nu_2/\nu_4$ +hot bands	120.	0.003	5	Cottaz et al 2000 Cottaz et al 2001	5 microns
700-1200	ν_2 +hot bands	568.	0.00005	2	Chen et al 1998, Belov et al 1980, 1998 Urban et al 1981, 2000	10 microns
19-40	rotation	441.	0.000002	2	Sasada et al. 1992 and many others !	

NH₃ ENERGY LEVELS

NH₃ energy levels



3 microns: not easy to observe from the Ground (CO₂ and H₂O telluric); ISO observations

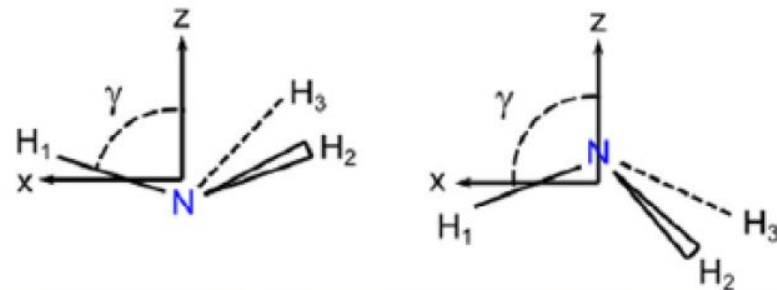
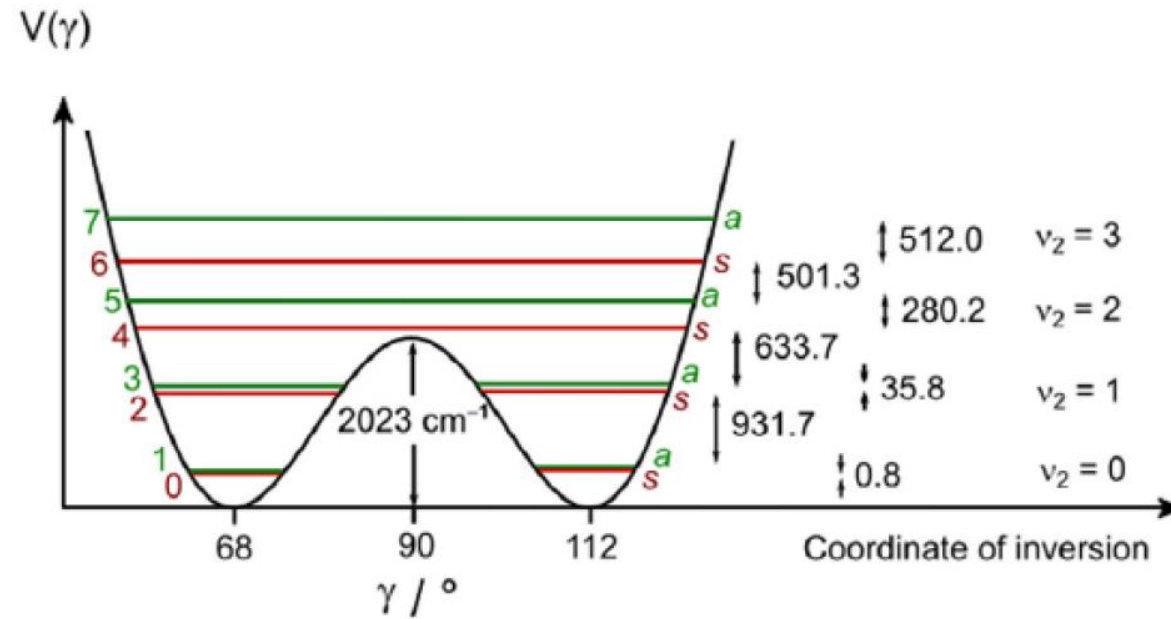
4 microns: hope to detect new elements

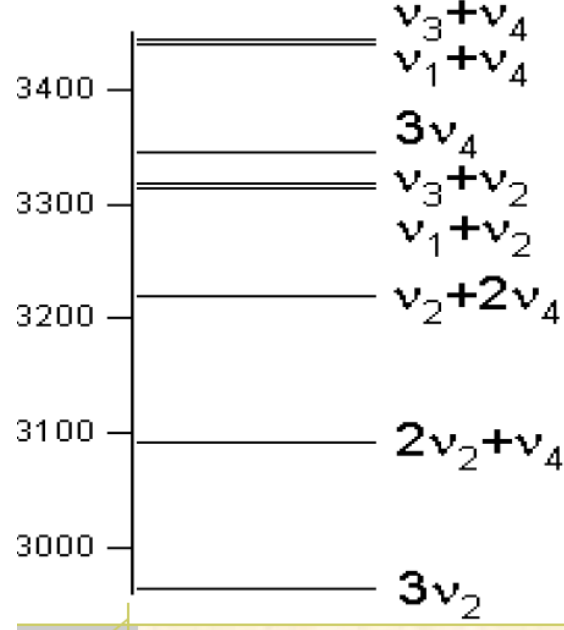
5 microns: probe deep (2-5 bars)

10 microns: probe upper troposphere and lower stratosphere (0.5-0.001 bars)

What makes NH_3 so hard???

Large amplitude motion : inversion





-The band $3v_2$:

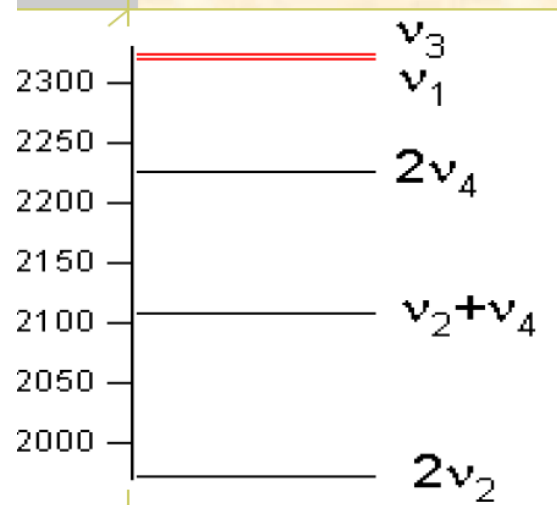
-Low resolution of line positions (Maki et al. JCP 1973)

- The octad bands:

New line positions and intensities measurements

(Butler et al., JMS 2006)

The Global analysis of the Dyad, pentad and octad bands: (Nikitin et al., JMS 2009)

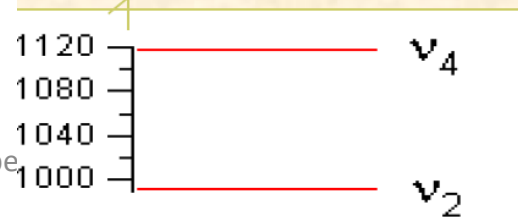


• The $2v_2/v_2+v_4/2v_4/v_1/v_3$ pentad:

-Frequencies: rms=0.009 cm⁻¹ up to J=16

(Tarrago et al. JMS, 1992, Ulenikov and al. JMS, 2002)

-Intensities: rms= 13% (Tarrago et al. JMS, 1992)



•The v_2/v_4 dyad:

-Frequencies: rms=0.0004cm⁻¹ up to J=22

(Fusina and al, J.Mol.Struc.,2000)

-Intensities: rms=2% (Brown and al., JMS, 2001)

-Linewidth: self **Broadening** coefficients

(J. Salem and al, JMS, 2004)

The pentad- 5 micron

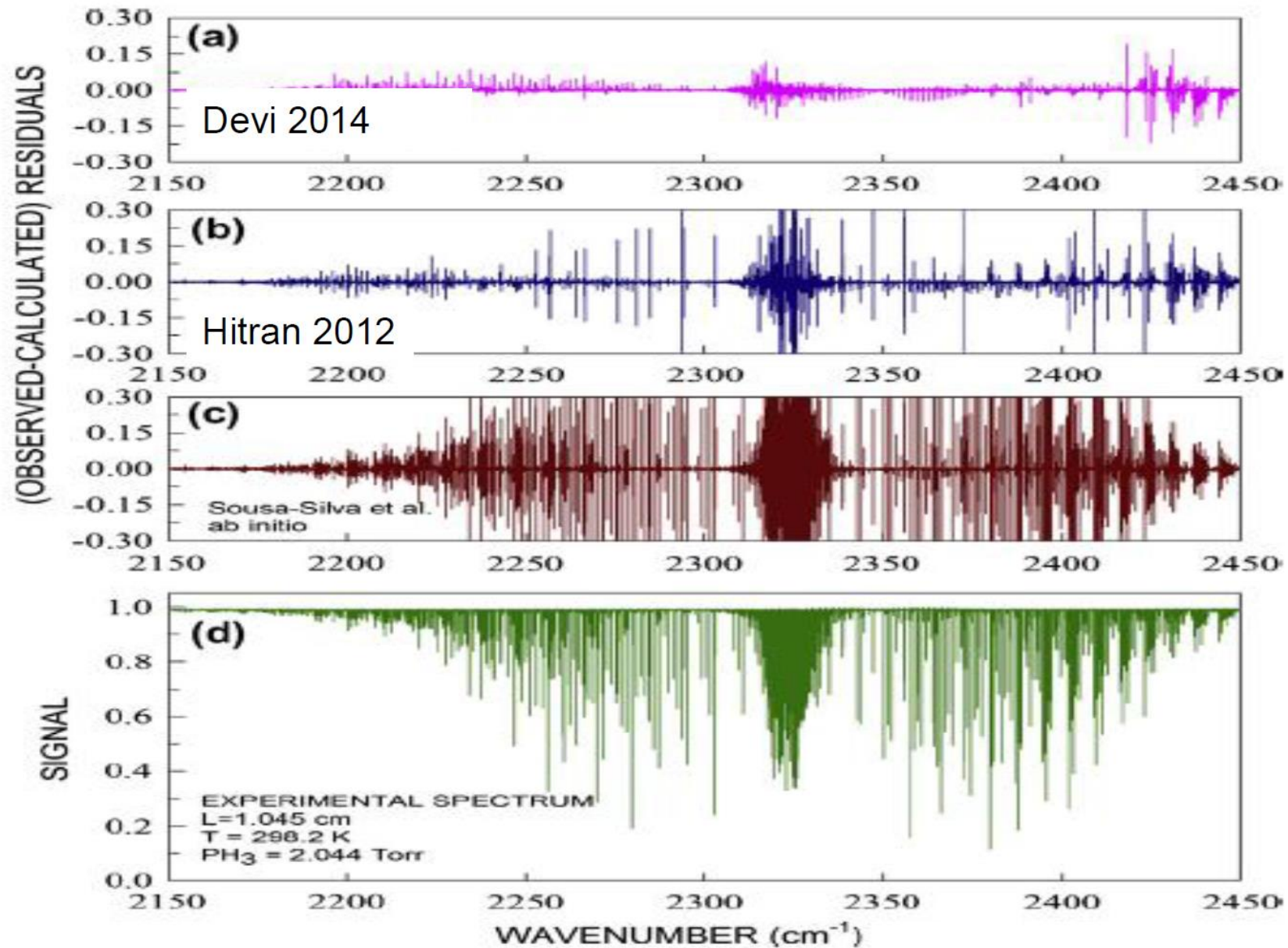
- Over **3400 line positions and 1750 intensities** measured and fitted in the pentad bands ($2\nu_2, \nu_2+\nu_4, 2\nu_4, \nu_1$ and ν_3 of PH₃) by analyzing 9 high-resolution room-temperature spectra recorded with two FTS spectrometers.

5 spectra recorded using the FT spectrometer at PNNL (short path of 1.045 cm) for the band intensities of the strong ν_1 and ν_3 fundamentals. **4 spectra recorded at Kitt Peak** for the weak $2\nu_2$ and $\nu_2+\nu_4$ (long path cell of 425 cm).

up to $J=14$ (rms = 0.00133 cm^{-1}), total line-list consists of 9894 transitions

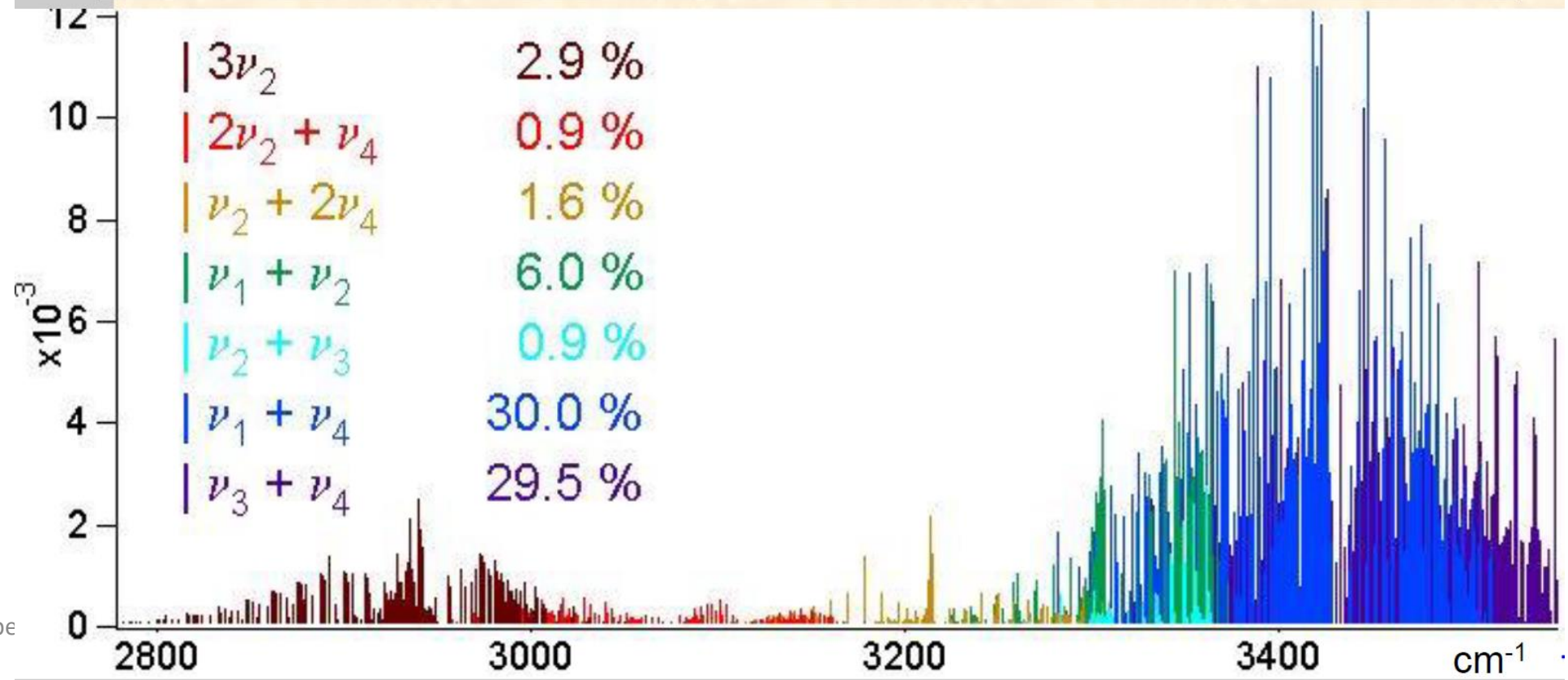
- **Our intensity measurements are about 7% higher than previous measurements. This cannot explain the 50% discrepancy observed in the vertical mixing ratios derived by astronomers ! → other effects: aerosol amounts ???**

Observed-calculated in the pentad region



ANALYSIS OF THE 3 MICRON REGION :

- Data 2750 - 3600 cm^{-1} : 8075 line positions and intensities obtained by L. R. Brown and R. Butler (Kitt Peak FTS, spectral resolution of 0.0115 cm^{-1}).
- Analysis of spectra: 4095 lines identified.
- 7 vibrational states simultaneously analysed
- **79% of intensity of region accounted for**, - Unassigned state is $3\nu_4$



Isotopes

Isotopes can be treated as regular molecular structures : isotopic ratios have no reason to be similar to Solar System values (Warning : terrestrial databases include the « standard » terrestrial ratio)

Special case : some isotopes change the symmetry of the molecule and can therefore have a very different spectroscopy – ex. CH_3D

Partition functions

Statistical physics

From the vibro-rotational calculations we have calculated the energy of upper level of each transition – this energy allows us to calculate the population of every level through Boltzmann statistics:

$$N_i = g_i e(-E_i/kT) / Z$$

Where Z is the partition function: Z = summation over all N_i

Emission and absorption coefficients

Calculation of transition probabilities =>

- * related to the molecular dipole momentum of the molecule
- Depends on the population of the emitting/absorbing level
- Basis : spontaneous, stimulated and absorption coefficients (Einstein coefficients)
- Emission and radiation : Einstein relations A_{ij} , B_{ij} , B_{ji}

Definition of line strength and absorption coefficients

See spectral line shapes course : Professor Ronald K. Hanson
<https://cefrc.princeton.edu/sites/g/files/toruqf1071/files/documents/Lecture%20Notes%20-%20Hanson.pdf>

Lorenz shapes (Collisions OR natural lines)
Gaussian shapes (Doppler thermal motions)

Far wings effects

Very strong lines can dominate the opacity very far from line center: the Lorentz line shape reaches the limit of validity when applied too far from line center

Hartmann et al, 2002

Biarritz, 2023 - Pierre Drossart

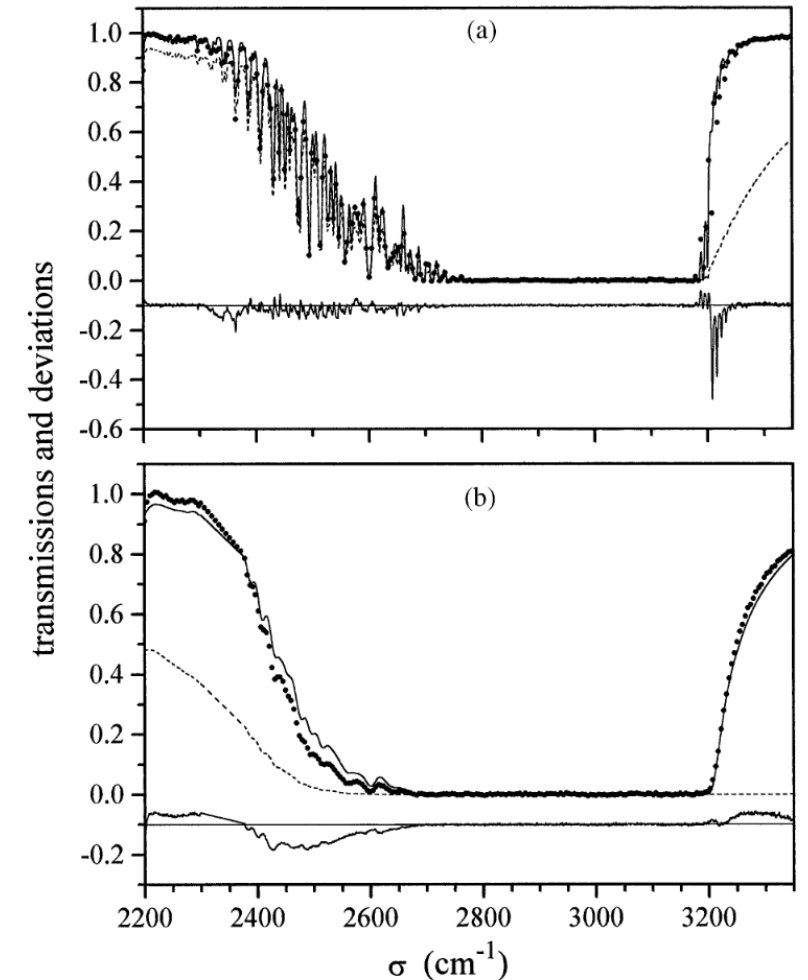
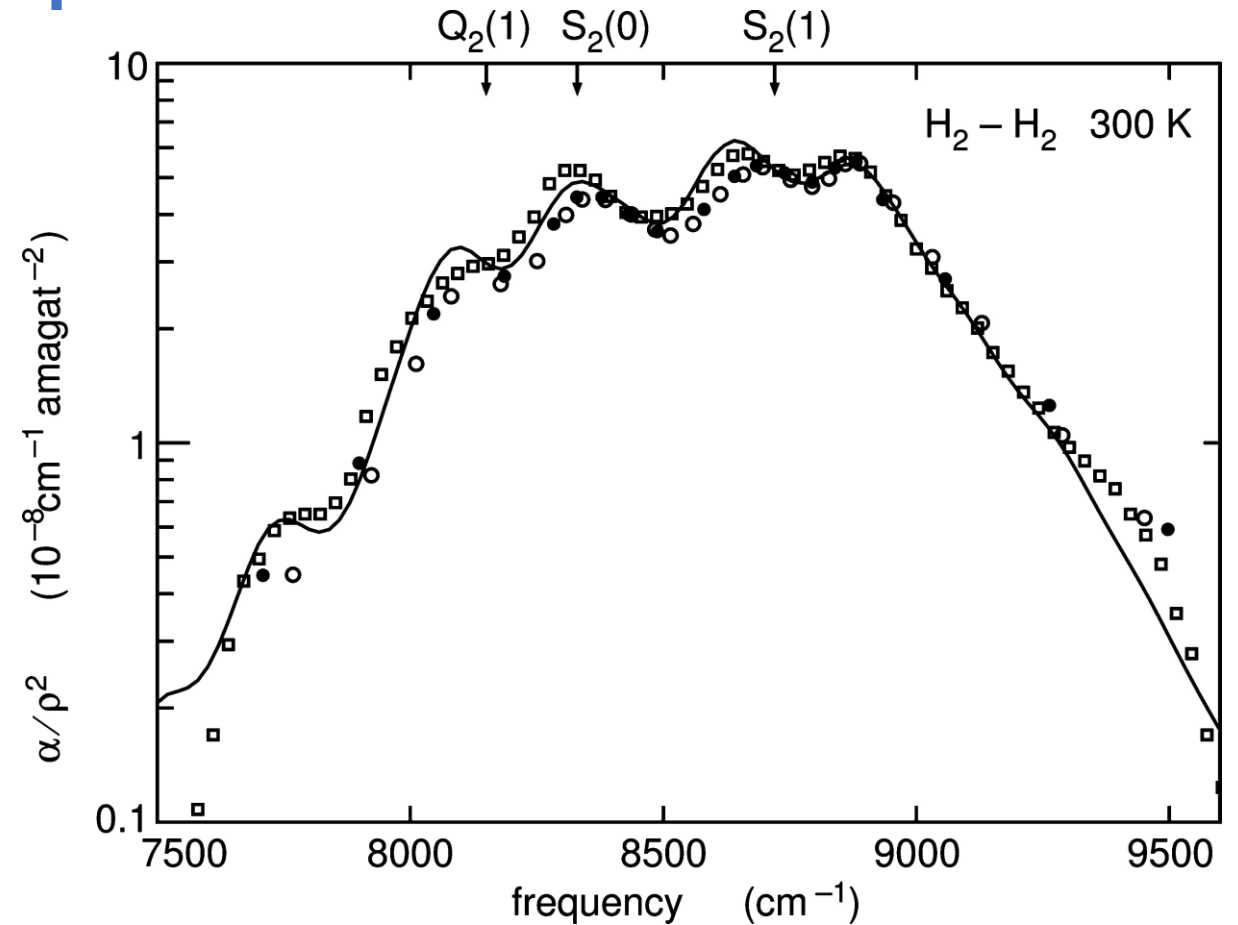


Fig. 1. Transmissions of $\text{CH}_4\text{-H}_2$ mixtures at room temperature (297 K) for a 3 m long path. \bullet are measured values. — and - - - have been calculated with the χ factor of Eq. (2) and purely Lorentzian line shapes ($\chi=1$), respectively. (a) $d_{\text{CH}_4}=0.919$ Am, $d_{\text{H}_2}=25.0$ Am. (b) $d_{\text{CH}_4}=1.84$ Am, $d_{\text{H}_2}=163$ Am. Measured-calculated residuals are given below the spectra.

Collision induced absorption

The continuum of atmospheric spectra, outside strong molecular bands, is dominated by quadrupolar effects from homopolar diatomic molecules like N_2 or H_2



Abel et al., J. Phys. Chem. A 2011, 115, 25, 6805–6812

Databases: how to compute a spectroscopic database ?

- Example = Hitran extraction
- How to retrieve the database ?
 - Schrödinger equation in Born-Oppenheimer approximation
 - Calculation of a database \Leftrightarrow calculation of the hamiltonian of the molecule
- Practical approaches :
 - combination of prediction/experiments \Rightarrow parametrized hamiltonian
 - Ab initio calculations
 - What is the necessary accuracy for practical use ?

International databases for spectroscopy

HITRAN (USA) , GEISA (France), JPL (USA), CDMS (Germany) ...

<https://hitran.org/> HITRAN is an acronym for high-resolution transmission molecular absorption database. HITRAN is a compilation of spectroscopic parameters that a variety of computer codes use to predict and simulate the transmission and emission of light in the atmosphere. (L. Rothman, Y. Gordon)



<https://geisa.aeris-data.fr/>

Developed by the ARA (Atmospheric Radiation Analysis) group at LMD (Laboratoire de Météorologie Dynamique, France)



GEISA (Gestion et Etude des Informations Spectroscopiques Atmosphériques: Management and Study of Atmospheric Spectroscopic Information), a computer accessible database system [Chédin et al. (1982), Husson et al. (1992), Jacquinet-Husson et al. (1999, 2005, 2008, 2011, 2016), Armante et al (2016), calculations of atmospheric radiative transfer, line-by-line and layer-by-layer approach

<http://vamdc.org>

International consortium VAMDC (Virtual Atomic and Molecular Data Centre

Databases : ExoMol

Tennyson et al,
JQSRT 2020

Mixture of ab
initio
calculations
and laboratory
data

ExoMol

H ₂	PH ₃	AlO	AlH	CS	HNO ₃	PN	H ₂ S	CrH	ScH	Done
LiH	OH	SO ₂	CH ₃ Cl	C ₂	BeH	PS	KCl	HCN	HNC	
HeH ⁺	NO	SH	HCl	CH ₄	NaCl	SiO	MgH	CH	CN	
H ⁺	O ₃	H ₂ CO	HDO	H ₂ O	NH ₃	CaH	SO ₃	CO	CO ₂	
H ₂ D ⁺	O ₂	HOOH	CH ₃ F	TiO	VO	FeH	CaO	C ₃	C ₂ H ₂	To-Do
NS	NaH	BaO	VN	CH ₃ D	YO	SiH ₄	PH	SH	C ₂ H ₄	
ZnS	P ₂ H ₂	SO	SiH	SiS	NiH	TiH	MgO	CH ₃ Cl	C ₂ H ₆	
	PH	PO				SiC		PS	C ₃ H ₈	

# The list of spectral lines. HITRAN-2004 format																					
# HITRAN. Molecule CH4. Isotopologue(s): 211.																					
# Wavenumber range: 2000.000000-4000.000000 cm-1, T: 296 K, P: 1 atm, Scut: 1e-20 cm/molecule																					
#MI	WN,cm-1	S,cm/mol	A,s-1	Lenv	Lself	El,cm-1	Nt	Pshift	GQNup	GQNlow	LQNup	LQNlow	Ierr	Iref	* SWup	SWlow					
61	2894.996098	1.109e-20	1.913e+01	.04700	.067	815.14360	.65-	.002000	0 0 1 0	1F2	0 0 0 0	1A1	11A2	15	12A1	2	765343463631	3 2 2	115.0	125.0	
61	2895.233319	1.102e-20	1.901e+01	.04950	.067	815.08900	.65-	.012300	0 0 1 0	1F2	0 0 0 0	1A1	11A1	14	12A2	1	765343463631	3 2 2	115.0	125.0	
61	2896.990180	1.116e-20	1.923e+01	.04760	.067	814.64600	.65-	.009250	0 0 1 0	1F2	0 0 0 0	1A1	11A2	16	12A1	1	765343463633	3 4 4	115.0	125.0	
61	2905.633661	1.132e-20	1.955e+01	.05000	.068	690.04920	.65-	.001200	0 0 1 0	1F2	0 0 0 0	1A1	10F2	41	11F1	3	765343463631	3 2 2	63.0	69.0	
61	2905.813742	1.140e-20	1.969e+01	.05000	.068	690.01740	.65-	.006000	0 0 1 0	1F2	0 0 0 0	1A1	10F1	39	11F2	3	765343464731	3 2 2	63.0	69.0	
61	2906.282471	1.106e-20	1.910e+01	.05410	.068	689.95670	.65-	.007700	0 0 1 0	1F2	0 0 0 0	1A1	10F2	42	11F1	2	765343463631	3 2 2	63.0	69.0	
61	2906.647628	1.110e-20	1.916e+01	.05360	.068	689.87670	.65-	.005000	0 0 1 0	1F2	0 0 0 0	1A1	10F1	40	11F2	2	765343463631	3 2 2	63.0	69.0	
61	2906.734957	1.859e-20	1.926e+01	.05380	.068	689.86210	.65-	.008520	0 0 1 0	1F2	0 0 0 0	1A1	10A1	15	11A2	1	765343463633	3 4 4	105.0	115.0	
61	2907.321273	1.141e-20	1.969e+01	.05020	.068	689.70750	.65-	.008960	0 0 1 0	1F2	0 0 0 0	1A1	10F1	41	11F2	1	765343463633	3 4 4	63.0	69.0	
61	2907.336088	1.141e-20	1.969e+01	.04980	.068	689.70520	.65-	.009000	0 0 1 0	1F2	0 0 0 0	1A1	10F2	43	11F1	1	765343463633	3 4 4	63.0	69.0	
61	2916.201625	1.836e-20	2.021e+01	.05910	.070	575.28520	.670	.000300	0 0 1 0	1F2	0 0 0 0	1A1	9F1	37	10F2	3	765343464731	3 2 2	57.0	63.0	
61	2916.301842	1.207e-20	1.992e+01	.04270	.070	575.27170	.64-	.005500	0 0 1 0	1F2	0 0 0 0	1A1	9E	24	10E	2	765343463631	3 2 2	38.0	42.0	
61	2916.396322	1.787e-20	1.967e+01	.05690	.070	575.25960	.67-	.011200	0 0 1 0	1F2	0 0 0 0	1A1	9F2	36	10F1	2	765343463631	3 2 2	57.0	63.0	
61	2916.753786	2.962e-20	1.956e+01	.05650	.070	575.22270	.67-	.008280	0 0 1 0	1F2	0 0 0 0	1A1	9A2	14	10A1	1	765343463633	3 4 4	95.0	105.0	
61	2916.966220	1.770e-20	1.948e+01	.05910	.070	575.18410	.67-	.004300	0 0 1 0	1F2	0 0 0 0	1A1	9F2	37	10F1	1	765343463631	3 2 2	57.0	63.0	
61	2917.066127	1.788e-20	1.968e+01	.05550	.070	575.16990	.67-	.008400	0 0 1 0	1F2	0 0 0 0	1A1	9F1	38	10F2	2	765343463631	3 2 2	57.0	63.0	
61	2917.629074	3.055e-20	2.017e+01	.05440	.070	575.05550	.67-	.008680	0 0 1 0	1F2	0 0 0 0	1A1	9A1	12	10A2	1	765343463631	3 2 2	95.0	105.0	
61	2917.652561	1.831e-20	2.015e+01	.04830	.070	575.05250	.67-	.002700	0 0 1 0	1F2	0 0 0 0	1A1	9F1	39	10F2	1	765343463631	3 2 2	57.0	63.0	
61	2917.662838	1.222e-20	2.017e+01	.04830	.070	575.05110	.64-	.005835	0 0 1 0	1F2	0 0 0 0	1A1	9E	25	10E	1	765343463631	3 2 2	38.0	42.0	
61	2926.700231	4.583e-20	2.051e+01	.06110	.073	470.87270	.67-	.000200	0 0 1 0	1F2	0 0 0 0	1A1	8A1	12	9A2	1	765343463631	3 2 2	85.0	95.0	
61	2926.782987	2.736e-20	2.040e+01	.05820	.073	470.86490	.67-	.007690	0 0 1 0	1F2	0 0 0 0	1A1	8F1	32	9F2	2	765343463633	3 4 4	51.0	57.0	
61	2926.885111	2.709e-20	2.020e+01	.05830	.073	470.85480	.67-	.007740	0 0 1 0	1F2	0 0 0 0	1A1	8F2	33	9F1	3	765343463633	3 4 4	51.0	57.0	
61	2927.076189	4.546e-20	2.034e+01	.05850	.073	470.83080	.67-	.007600	0 0 1 0	1F2	0 0 0 0	1A1	8A2	10	9A1	1	765343463633	3 4 4	85.0	95.0	
61	2927.372646	2.682e-20	2.000e+01	.05750	.073	470.80510	.67-	.008040	0 0 1 0	1F2	0 0 0 0	1A1	8F2	34	9F1	2	765343463633	3 4 4	51.0	57.0	
61	2927.429168	1.800e-20	2.014e+01	.05000	.073	470.79880	.65-	.005800	0 0 1 0	1F2	0 0 0 0	1A1	8E	23	9E	1	764332	53638	7 1 7	34.0	38.0
61	2927.932131	2.765e-20	2.062e+01	.06330	.073	470.72020	.67-	.008390	0 0 1 0	1F2	0 0 0 0	1A1	8F1	33	9F2	1	765343463631	3 2 2	51.0	57.0	
61	2927.963557	2.765e-20	2.062e+01	.05370	.073	470.71680	.67-	.008480	0 0 1 0	1F2	0 0 0 0	1A1	8F2	35	9F1	1	765343463633	3 4 4	51.0	57.0	
61	2937.234649	3.880e-20	2.091e+01	.05500	.074	376.82610	.72-	.006700	0 0 1 0	1F2	0 0 0 0	1A1	7F1	30	8F2	2	765343463631	3 2 2	45.0	51.0	
61	2937.308180	2.571e-20	2.079e+01	.04770	.074	376.82110	.69-	.005200	0 0 1 0	1F2	0 0 0 0	1A1	7E	19	8E	2	765343463631	3 2 2	30.0	34.0	
61	2937.495038	3.853e-20	2.077e+01	.05680	.074	376.80460	.72-	.002000	0 0 1 0	1F2	0 0 0 0	1A1	7F2	28	8F1	2	765343463631	3 2 2	45.0	51.0	
61	2937.767224	3.817e-20	2.058e+01	.05890	.074	376.78570	.72-	.006700	0 0 1 0	1F2	0 0 0 0	1A1	7F1	31	8F2	1	765343463631	3 2 2	45.0	51.0	
61	2938.192639	2.606e-20	2.107e+01	.05890	.074	376.73550	.69-	.001000	0 0 1 0	1F2	0 0 0 0	1A1	7E	20	8E	1	765343463631	3 2 2	30.0	34.0	
61	2938.215410	3.910e-20	2.108e+01	.05610	.074	376.73360	.72-	.008360	0 0 1 0	1F2	0 0 0 0	1A1	7F2	29	8F1	1	765343463633	3 4 4	45.0	51.0	
61	2938.251832	6.530e-20	2.112e+01	.05250	.074	376.73030	.72-	.008000	0 0 1 0	1F2	0 0 0 0	1A1	7A2	11	8A1	1	765343463631	3 2 2	75.0	85.0	
61	2947.667995	5.128e-20	2.139e+01	.05710	.075	293.17850	.73-	.005100	0 0 1 0	1F2	0 0 0 0	1A1	6F2	26	7F1	2	765343463631	3 2 2	39.0	45.0	
61	2947.810950	3.406e-20	2.131e+01	.04850	.075	293.17000	.70-	.005100	0 0 1 0	1F2	0 0 0 0	1A1	6E	17	7E	1	765343463631	3 2 2	26.0	30.0	
61	2947.912105	5.069e-20	2.114e+01	.06340	.075	293.16440	.73-	.003800	0 0 1 0	1F2	0 0 0 0	1A1	6F1	24	7F2	2	765343463631	3 2 2	39.0	45.0	
61	2948.107945	8.412e-20	2.105e+01	.05990	.075	293.15410	.73-	.007090	0 0 1 0	1F2	0 0 0 0	1A1	6A1	10	7A2	1	765343463631	3 2 2	65.0	75.0	
61	2948.421423	5.149e-20	2.148e+01	.06340	.075	293.12640	.73-	.003800	0 0 1 0	1F2	0 0 0 0	1A1	6F1	25	7F2	1	765343463631	3 2 2	39.0	45.0	
61	2948.474107	5.171e-20	2.157e+01	.05780	.075	293.12290	.73-	.006880	0 0 1 0	1F2	0 0 0 0	1A1	6F2	27	7F1	1	765343463631	3 2 2	39.0	45.0	

Application to exoplanets

The spectroscopy of exoplanets collect the most challenging parts for spectroscopy : high temperatures (\Rightarrow high J, hot vibrational bands), large number of molecules and complex atmospheric structures

Difficulties for high temperature spectra

- Large number of overtones
- Accuracy of the database (missing bands, accuracy of coefficients at high temperatures)

The need for continued research in cooperation with spectroscopic group is mandatory to adapt the needs of exoplanets community with spectroscopic research !